

Adiabatic dynamics of quantum many-body systems

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Overview

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Quantum Adiabatic Theorem

Quantum Adiabatic Theorem (QAT) – colloquially:

A system evolving under a time-dependent Hamiltonian can be kept arbitrarily close to the Hamiltonian's instantaneous ground state provided that the parameters of the Hamiltonian vary *slowly enough*.

Key question: What is the exact meaning of “*slowly enough*”?

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- adiabatic quantum computers and quantum annealers
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- Quantum Field Theory
- *etc*

Notations and definitions

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- Simplest case: linear driving, $\lambda(t) = \Gamma t$, Γ being the driving rate. In general, $\Gamma = \partial\lambda/\partial t$.
- Use λ instead of t as the evolution parameter. Schrodinger equation:

$$i\Gamma \frac{\partial}{\partial \lambda} \Psi_\lambda = \hat{H}_\lambda \Psi_\lambda.$$

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- One calls the evolution adiabatic as long as Ψ_λ remains close to Φ_λ , or in other words if the fidelity

$$\mathcal{F}(\lambda) = |\langle \Phi_\lambda | \Psi_\lambda \rangle|^2$$

is close to one.

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Under closer investigation, two complementary questions can be posed:

Q1. For a given driving rate Γ , how long the adiabaticity can be maintained with a given accuracy ε ?

Q2. How small should the driving rate Γ be for a given target λ and a given accuracy ε ?

Orthogonality catastrophe

Orthogonality catastrophe – colloquially:

Given a many-body Hamiltonian \hat{H}_λ , two ground states corresponding to slightly different λ 's can become nearly orthogonal with growing size of the system, N [Anderson, 1967].

Orthogonality catastrophe

Orthogonality catastrophe – rigorously. *Orthogonality overlap* in the leading order in λ :

$$\mathcal{C}(\lambda) \equiv |\langle \Phi_\lambda | \Phi_0 \rangle|^2 = e^{-C_N \lambda^2}.$$

The orthogonality catastrophe takes place whenever $C_N \rightarrow \infty$ in the thermodynamic limit (TL), $N \rightarrow \infty$. The behavior of C_N is determined by the type of driving and the gap.

Orthogonality catastrophe: scaling

$$C(\lambda) \equiv |\langle \Phi_\lambda | \Phi_0 \rangle|^2 = e^{-C_N \lambda^2}.$$

| | Local driving | Bulk driving |
|-----------------|---|--------------|
| gapless systems | $C_N \sim \log N$ | $C_N \sim N$ |
| gapped systems | $\lim_{N \rightarrow \infty} C_N$ is finite | $C_N \sim N$ |

Key idea

In a many-body system subject to orthogonality catastrophe

$$\mathcal{F}(\lambda) \simeq \mathcal{C}(\lambda)$$

up to times sufficiently long for the adiabaticity to completely break down.

Central result

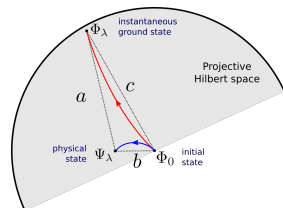
$$|\mathcal{F}(\lambda) - \mathcal{C}(\lambda)| \leq \mathcal{R}_\lambda$$

$$\mathcal{R}_\lambda \equiv \Gamma^{-1} \int_0^\lambda \sqrt{\langle \hat{H}_{\lambda'}^2 \rangle_0 - \langle \hat{H}_{\lambda'} \rangle_0^2} d\lambda',$$

where $\langle \dots \rangle_0 \equiv \langle \Psi_0 | \dots | \Psi_0 \rangle$.

For $\hat{H}_\lambda = \hat{H}_0 + \lambda \hat{V}$, one gets a simplified \mathcal{R}_λ :

$$\mathcal{R}_\lambda = \lambda^2 \delta V_N / (2\Gamma) \quad \text{with} \quad \delta V_N \equiv \sqrt{\langle \hat{V}^2 \rangle_0 - \langle \hat{V} \rangle_0^2}.$$



OL, O. Gamayun, V. Cheianov
PRL 119, 200401 (2017)

Adiabaticity breakdown time (Question 1)

Define the adiabaticity breakdown time t_* and parameter $\lambda_* \equiv \lambda(t_*)$:

$$\mathcal{F}(\lambda_*) = \frac{1}{e}.$$

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Relation between adiabaticity and orthogonality catastrophe implies

$$\lambda_* = 1/\sqrt{C_N}$$

up to small corrections, as long as $\mathcal{R}(C_N^{-1/2}) \ll 1$. The latter is guaranteed for sufficiently large system since

$$\frac{\delta V_N}{C_N} \rightarrow 0 \quad \text{for} \quad N \rightarrow \infty.$$

Necessary condition for many-body adiabaticity (Q 2)

If the orthogonality catastrophe is present, the adiabaticity can be maintained for finite systems only as long as $\mathcal{R}(\lambda_*)$ is large enough to make inequality

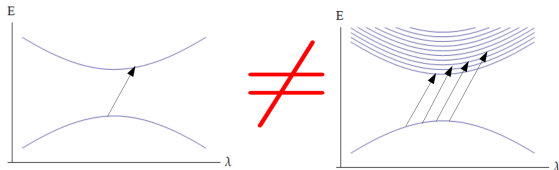
$$|\mathcal{F}(\lambda) - \mathcal{C}(\lambda)| \leq \mathcal{R}_\lambda$$

trivial.

This entails a **necessary adiabatic condition**:

$$\Gamma_N < \frac{\delta V_N}{2C_N} \frac{1}{1 - e^{-1} - \varepsilon}.$$

Adiabaticity and a gap



In a two-level system adiabaticity is governed by the gap (Landau-Zener). The adiabatic condition:

$$\Gamma \ll \Delta E_{\min}.$$

A Landau-Zener-type guess is typically **completely wrong** for bulk driven many-body systems! The adiabatic condition:

$$\Gamma \ll f_N \Delta E_{\min} \quad \text{with} \quad \lim_{N \rightarrow \infty} f_N = 0.$$

Take-home message

Maintaining adiabaticity in a many-body system is challenging.

Even more challenging than one may assume based on naive considerations employing energy gap.

Application to Grover adiabatic search

Adiabatic quantum computation:

$$H_t = \left(1 - \frac{t}{T}\right) H_0 + \frac{t}{T} H_P$$

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This scaling reproduces the scaling of the explicitly known optimal run time.

OL, Journal of Russian Laser Research 2018

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Genuine many-body adiabaticity is a *sufficient* condition for a plethora of "adiabatic" phenomena (quantized transport, quasi-Bloch oscillations, adiabatic quantum computation *etc*).

But is it really *necessary*?

Thermodynamic adiabaticity

Thermodynamic adiabaticity (see e.g. Polkovnikov, Gritsev, Nature Phys. 2008):

energy gaps between levels $\ll \Gamma \ll$ all intensive energy scales

Thermodynamic vs genuine adiabaticity

For gapped spin systems *thermodynamic adiabaticity* is enough for expectation values of local operators to stay close to their ground state values, even if the *genuine adiabaticity* is already broken (Bachmann, De Roeck, Fraas PRL 2017).

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Can it be that the genuine adiabaticity is completely irrelevant in the many-body setting?

This is not always the case!

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In fact, whether the thermodynamic adiabaticity is enough for an “adiabatic” phenomenon to occur, or a genuine many-body adiabaticity is necessary, is a tricky question.

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We consider dynamics of an impurity in a 1D quantum fluid as an examples.

Mobile impurity in a 1D fluid

A mobile impurity particle in a translation-invariant 1D gas of N fermions



$$\hat{H}_t = \frac{P^2}{2m} + \sum_{n=1}^N \frac{p_n^2}{2m} + g_t \sum_{i=1}^N \delta(x_i - x)$$

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Coupling is slowly switched on up to a value g :

$$g_t = \Gamma t (k_F/m), \quad t \in [0, \tau], \quad g_\tau \equiv g$$

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Genuine many-body adiabaticity:

$$\Gamma \ll \Delta E \lesssim E_F/N$$

Thermodynamic adiabaticity:

$$E_F/N \ll \Gamma \ll E_F$$

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Will the local physical observables at $t \gg \tau$ differ?

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Local observable: v_∞ (velocity of the impurity at $t = \infty$).

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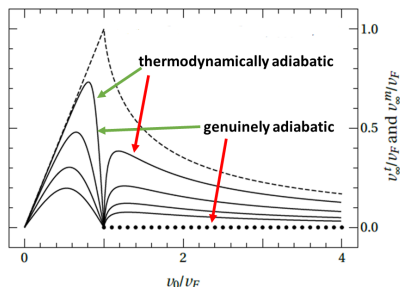
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$$v_0 < v_F:$$

$$v_\infty^{\text{thermodynamic}} = v_\infty^{\text{genuine}}$$

$$v_0 > v_F:$$

$$v_\infty^{\text{genuine}} = 0$$

$$v_\infty^{\text{thermodynamic}} > 0$$

Gamayun, OL *et al* PRL 2018

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One can enquire about adiabaticity at a finite temperature:

$$i\partial_t \rho_t = [H_t, \rho_t]$$

$$\rho_0 = e^{-\beta H_0} / Z_0 \quad Z_0 \equiv \text{tr} e^{-\beta H_0}$$

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$$\|\rho_t - \rho_t^\beta\| = ?$$

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So what happens at a finite temperature?

Unitarily driven systems

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Adiabatic theorem at a finite temperature

For $U_t = e^{i\omega t V}$

$$\|\rho_t - \rho_t^\beta\|_H \leq 2\omega\beta\sqrt{\langle V^2 \rangle_\beta} \left(1 + \sqrt{2}(\omega t)\sqrt{\langle V^2 \rangle_\beta}\right)$$

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Polynomial system size dependence for global driving ($\langle V^2 \rangle_\beta \sim N$)!

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- Contrary to the common belief, whenever driving is of bulk type, **even a finite gap is not able to protect adiabaticity in the thermodynamic limit!**
- Necessary adiabatic condition for finite systems derived – the most stringent to date, to the best of our knowledge!

Summary and outlook II

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- For others, genuine many-body adiabaticity is strictly necessary.
- The discrimination between the two scenarios is subtle and is currently done on the case-by-case basis. General theoretical understanding is lacking!
- Adiabatic theorem at finite temperature is proven for a particular class of time-dependent Hamiltonians. Energy gaps do not enter!

Thank you for your attention!