

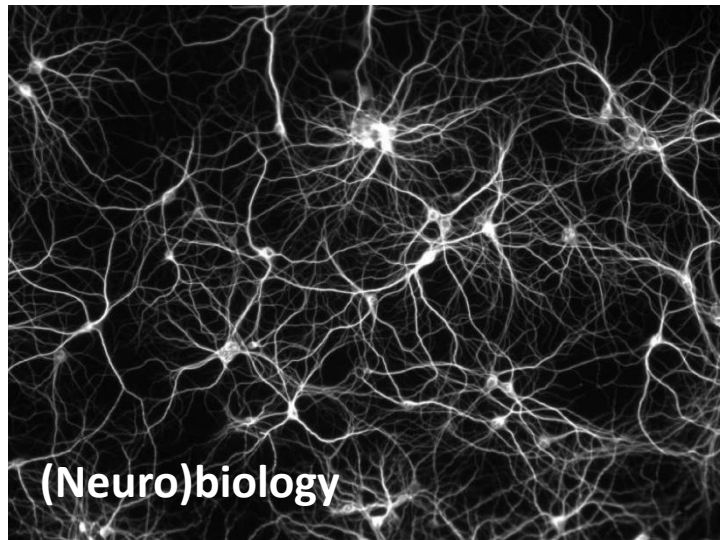
Molecular dynamics in ice and water:

insights from broadband dielectric spectroscopy

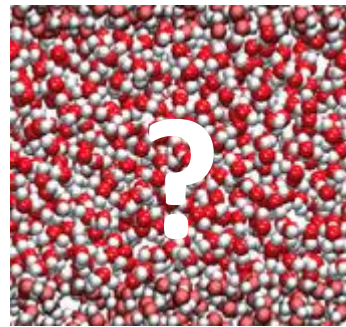
Vasily G. Artemov

5 August, 2021

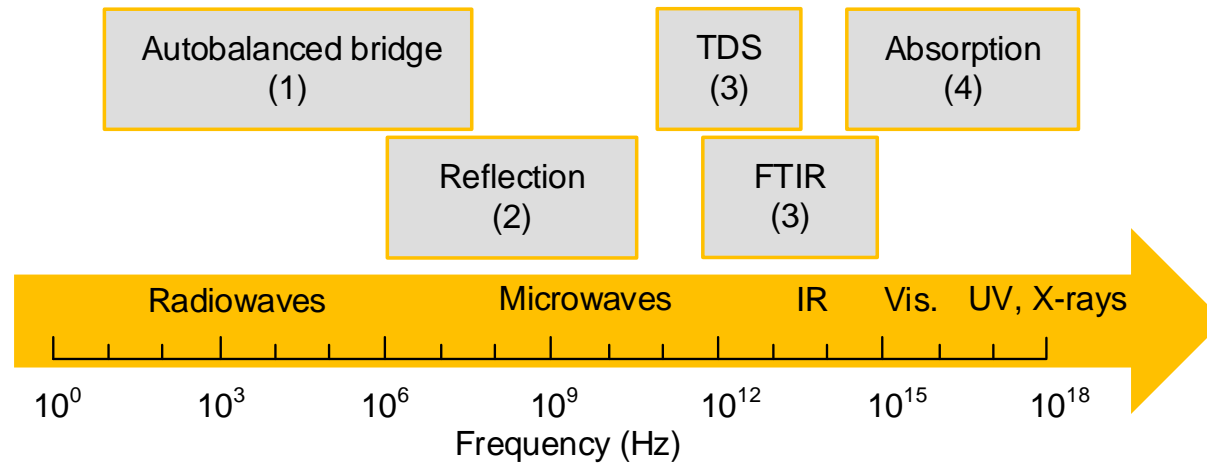
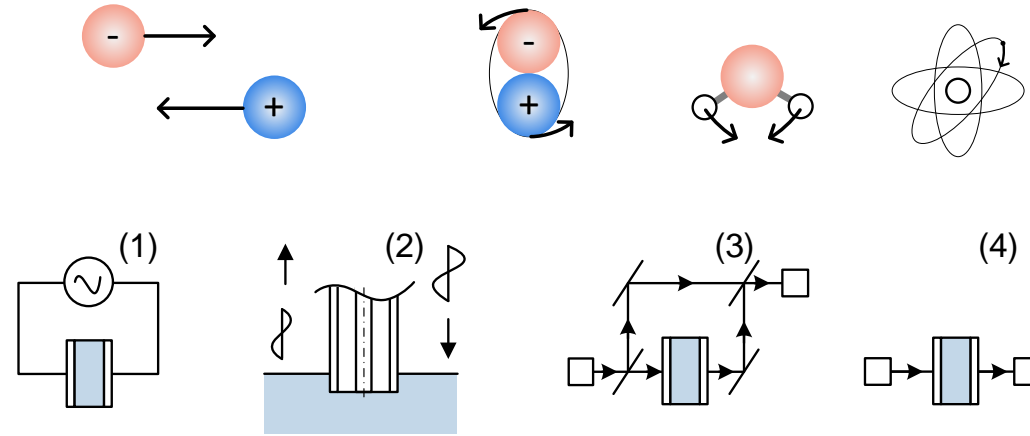
Motivation



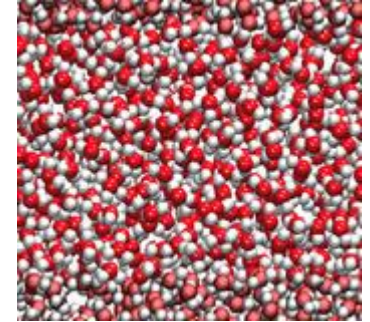
Structure & Dynamics



Broadband dielectric spectroscopy



Molecular dielectric



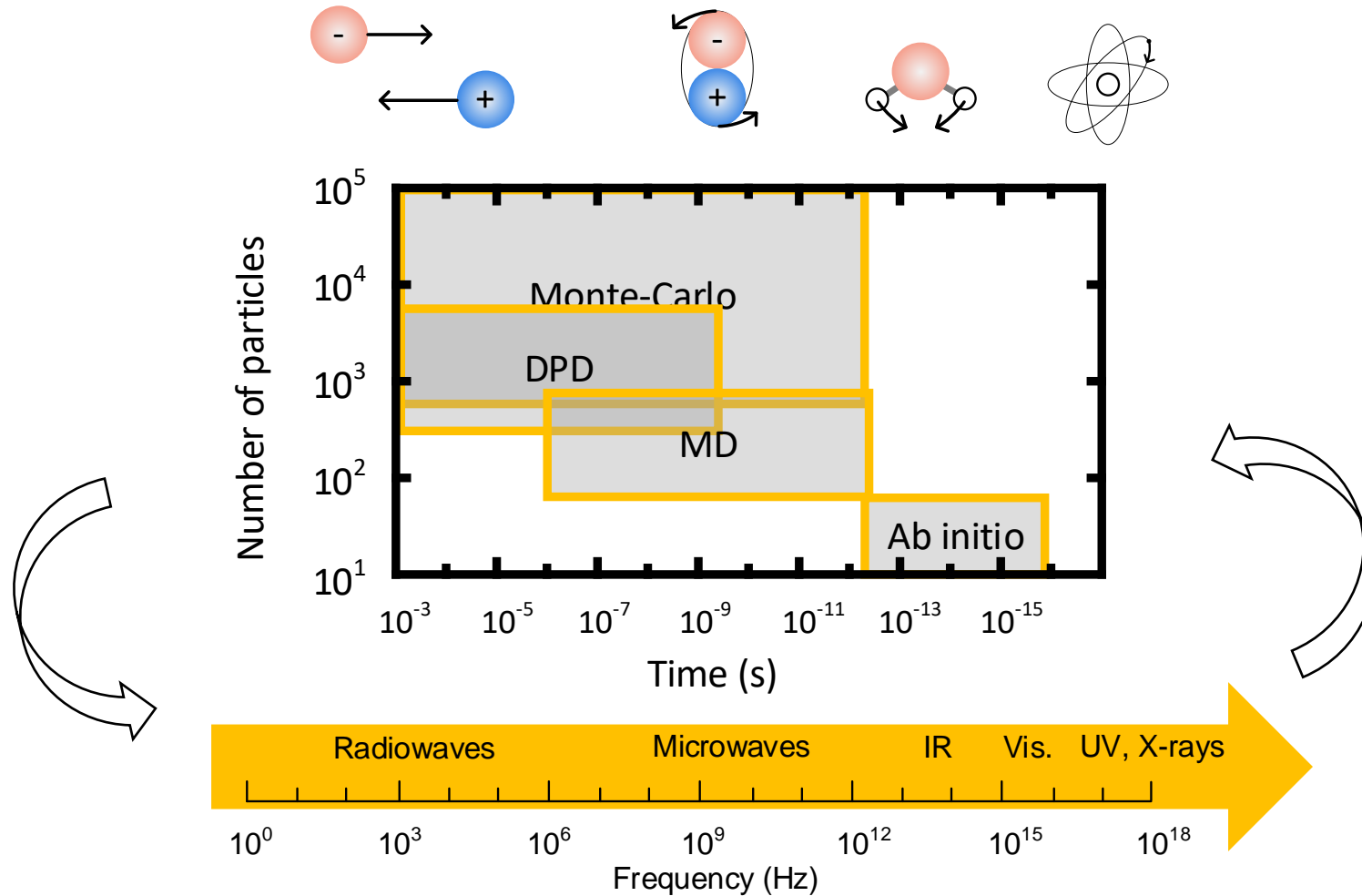
Maxwell's Equations

$$\begin{aligned} \nabla \times \mathbf{E} &= -\frac{\partial \mathbf{B}}{\partial t} \\ \nabla \times \mathbf{H} &= \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t} \\ \nabla \cdot \mathbf{D} &= \rho \\ \nabla \cdot \mathbf{B} &= 0 \end{aligned}$$

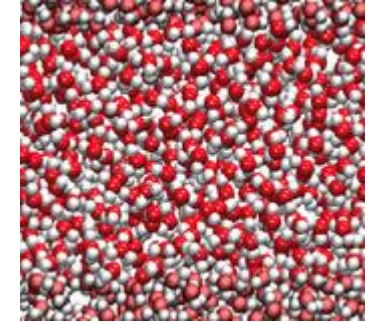
Constitutive relation

$$\mathbf{D}(\mathbf{r}, \omega) = \epsilon(\omega) \mathbf{E}(\mathbf{r}, \omega)$$

Broadband dielectric spectroscopy and molecular dynamics simulations



Molecular dielectric



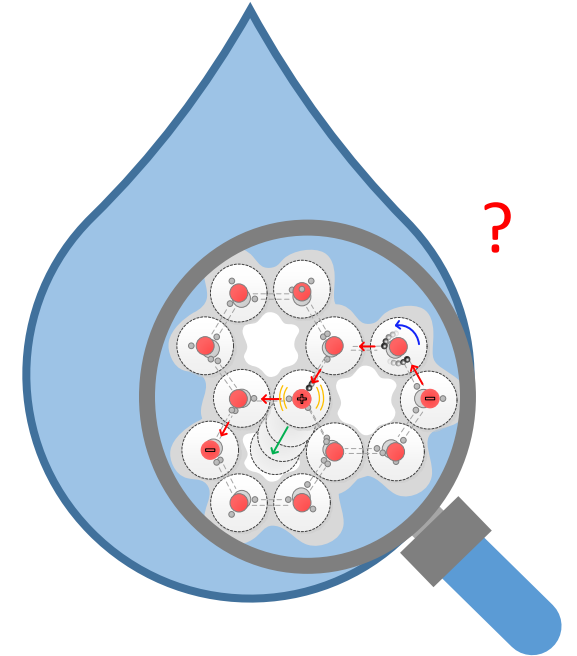
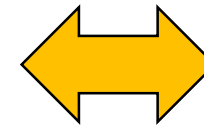
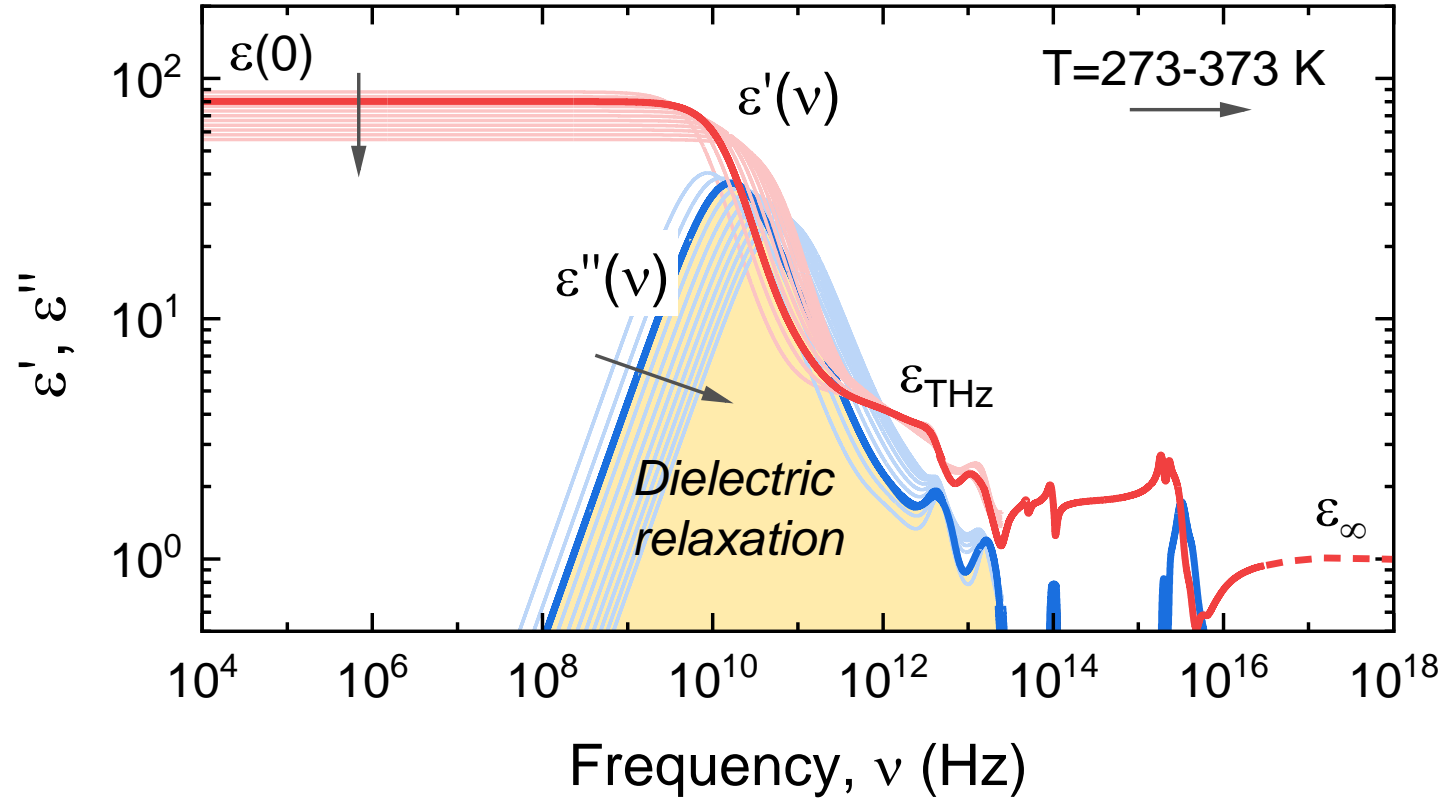
Maxwell's Equations

$$\begin{aligned} \nabla \times \mathbf{E} &= -\frac{\partial \mathbf{B}}{\partial t} \\ \nabla \times \mathbf{H} &= \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t} \\ \nabla \cdot \mathbf{D} &= \rho \\ \nabla \cdot \mathbf{B} &= 0 \end{aligned}$$

Constitutive relation

$$\mathbf{D}(\mathbf{r}, \omega) = \epsilon(\omega) \mathbf{E}(\mathbf{r}, \omega)$$

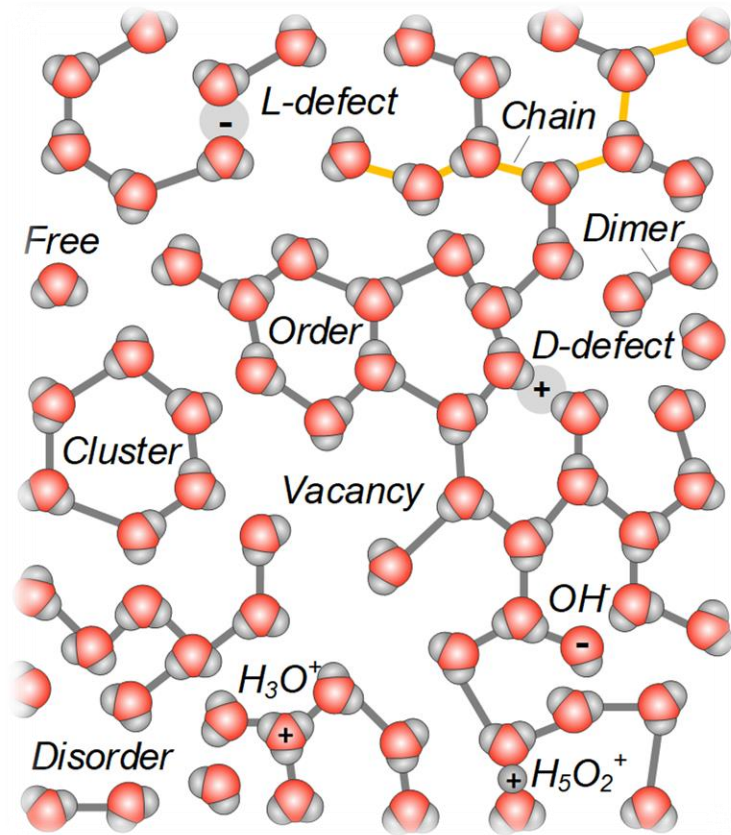
Broadband dielectric spectrum of water



$$D(\mathbf{r}, \omega) = \epsilon(\omega) E(\mathbf{r}, \omega)$$

Bernal-Fowler water (1933)

Where did we get this structure of water?



THE JOURNAL OF CHEMICAL PHYSICS

VOLUME 1

AUGUST, 1933

NUMBER 8

A Theory of Water and Ionic Solution, with Particular Reference to Hydrogen and Hydroxyl Ions

J. D. BERNAL AND R. H. FOWLER, *University of Cambridge, England*

(Received April 29, 1933)

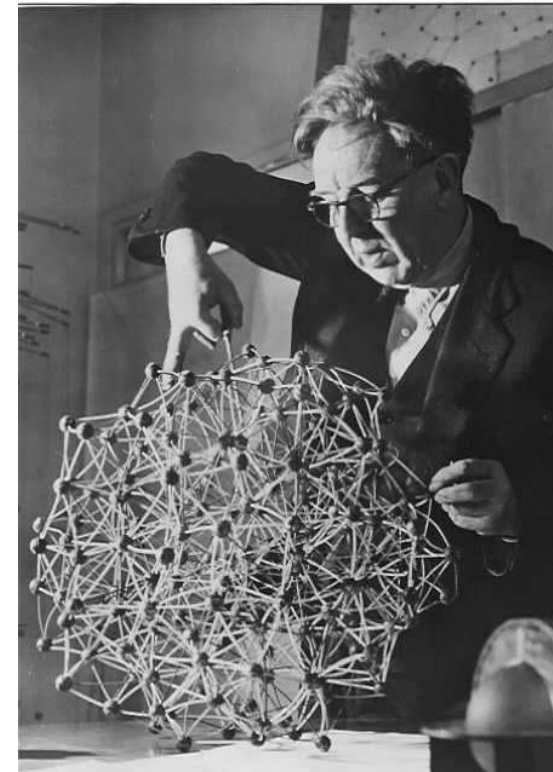
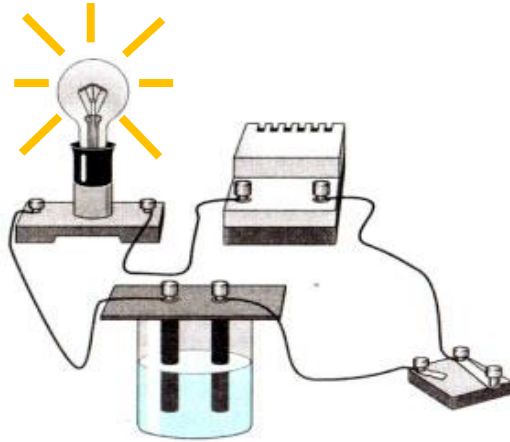


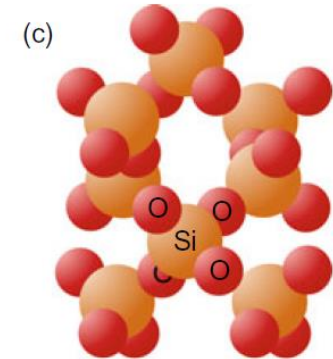
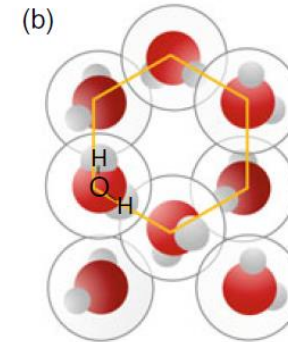
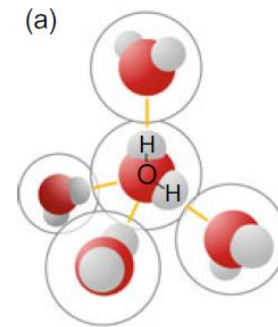
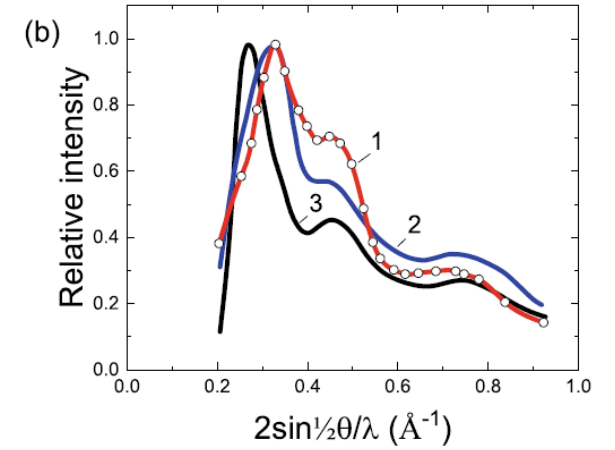
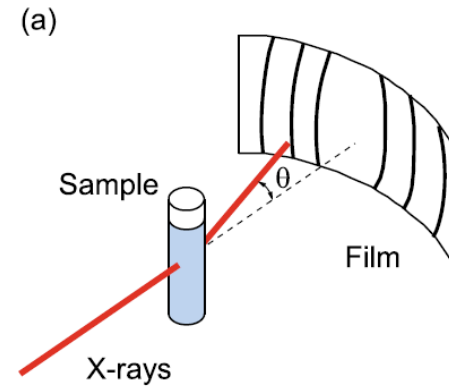
Photo from: J. L. Finney, *J. Phys.: Conf. Ser.* 57, 4 (2007)

Bernal-Fowler water (1933): experimental background



Assumption #1:

Pure water is a poor conductor, thus it has low concentration of H^+ and OH^- .



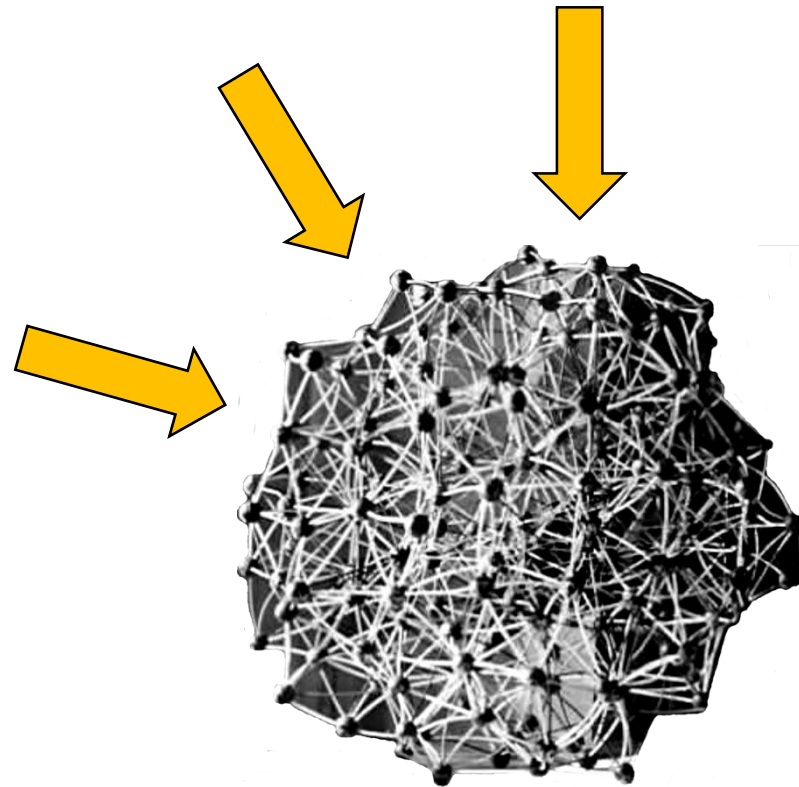
Assumption #2:

Water scatters X-rays just like quartz, thus, it has similar structure.

Test of Bernal-Fowler water

1933 - 2021

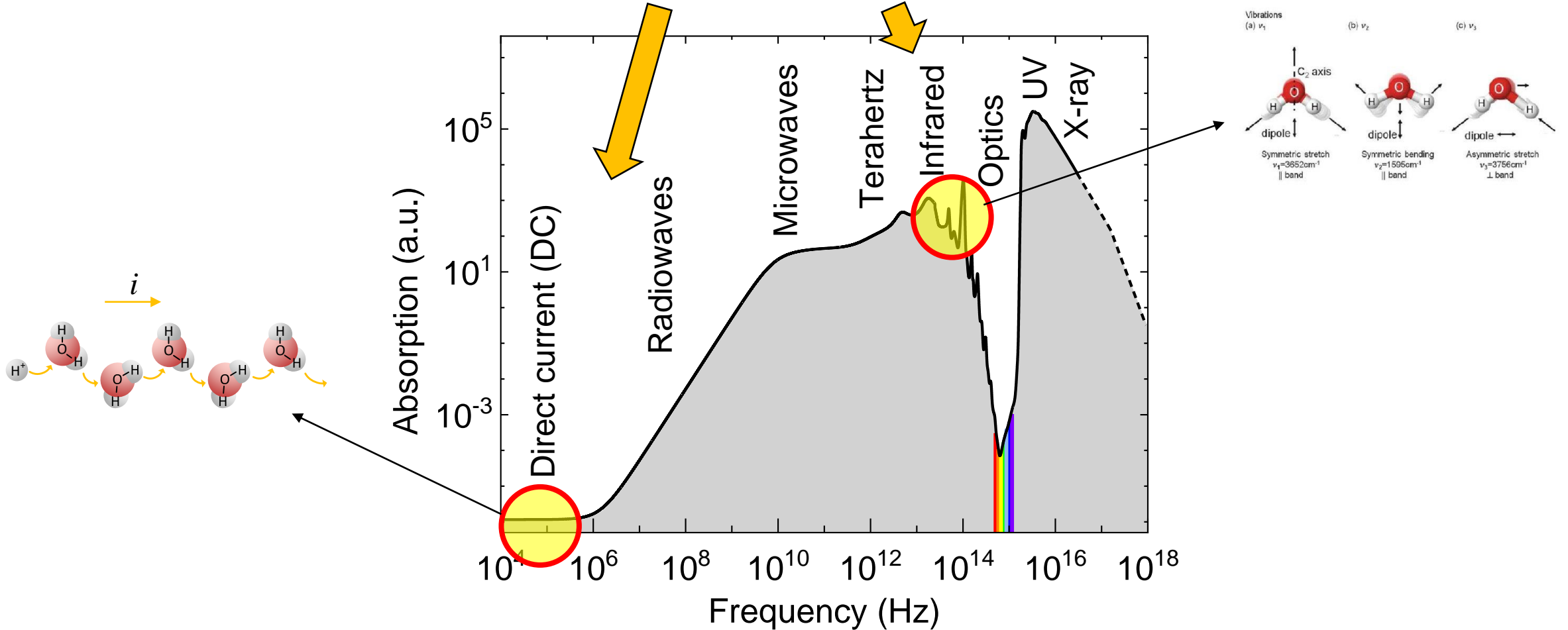
- Ab-initio, Monte Carlo and Molecular dynamics simulations
- Diffusion measurements with isotopic tracers
- NMR spectroscopy
- Neutron Scattering
- X-ray scattering



What about electrostatics?

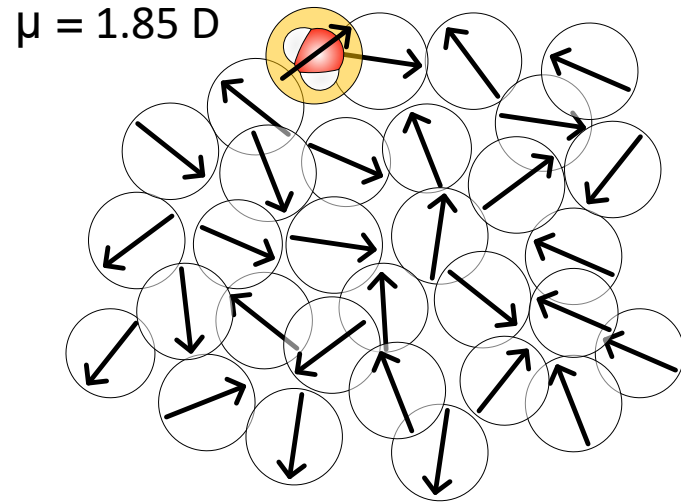
Absorption of electromagnetic waves by water

Range of validity of the Bernal-Fowler model

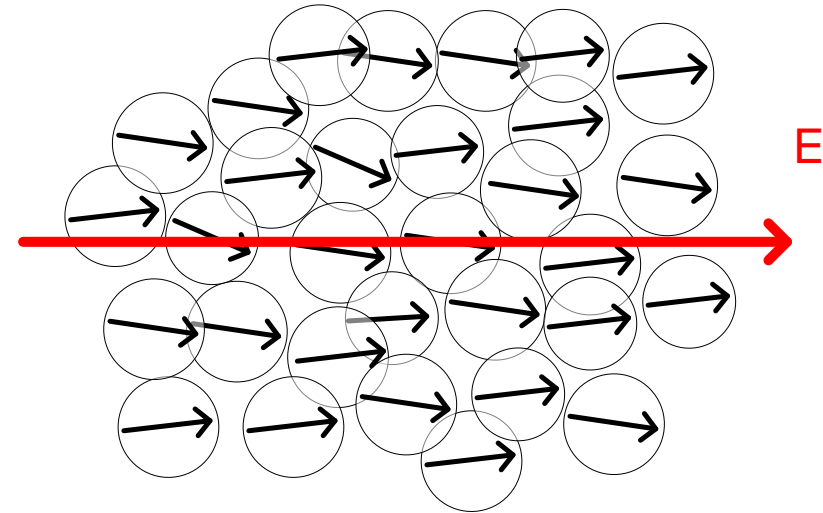


Bernal-Fowler water in electric field

$E=0$



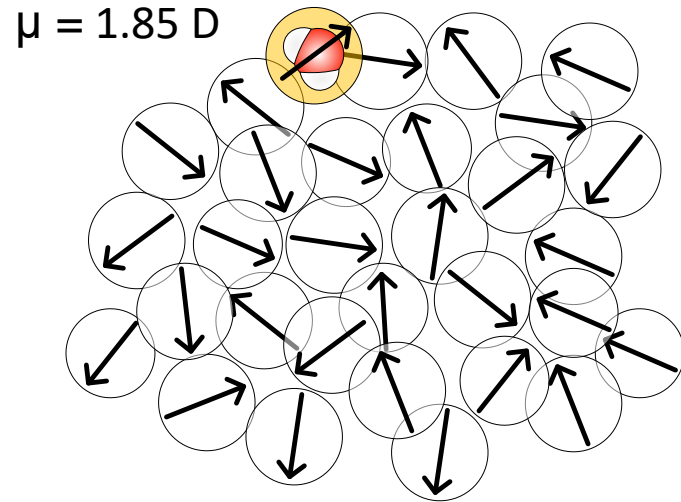
$E>0$



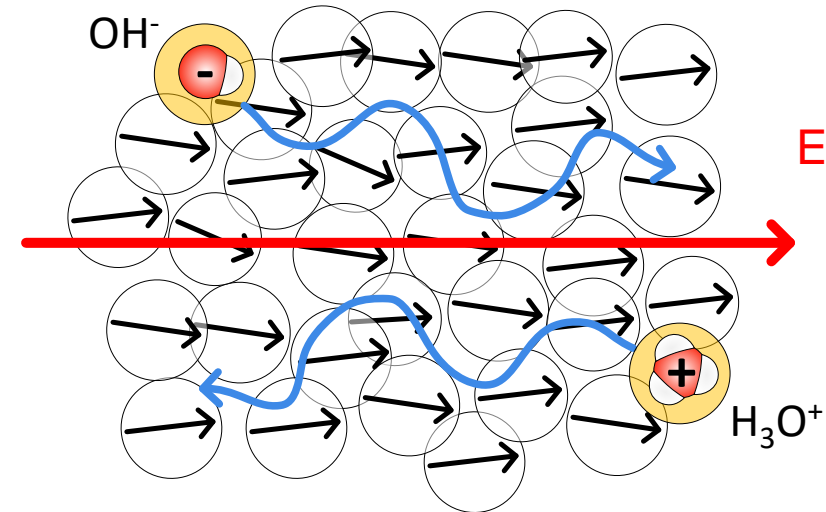
Dielectric constant: $\epsilon(0) = 1 + \frac{4\pi N\mu^2}{3Vk_B T}$ \Rightarrow $\epsilon(0)_{calc} \approx 14$ \longleftrightarrow $\epsilon(0)_{exp} \approx 80$

Bernal-Fowler water in electric field

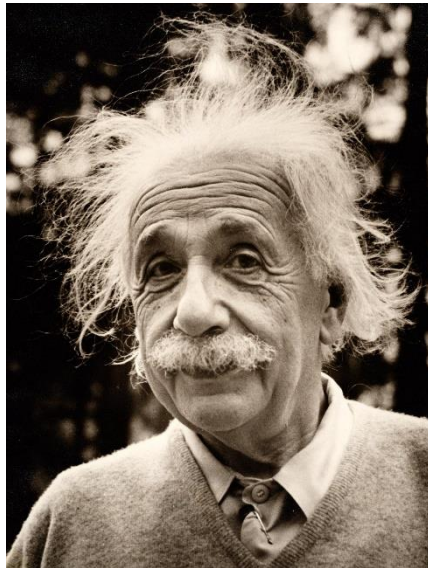
$E=0$



$E>0$

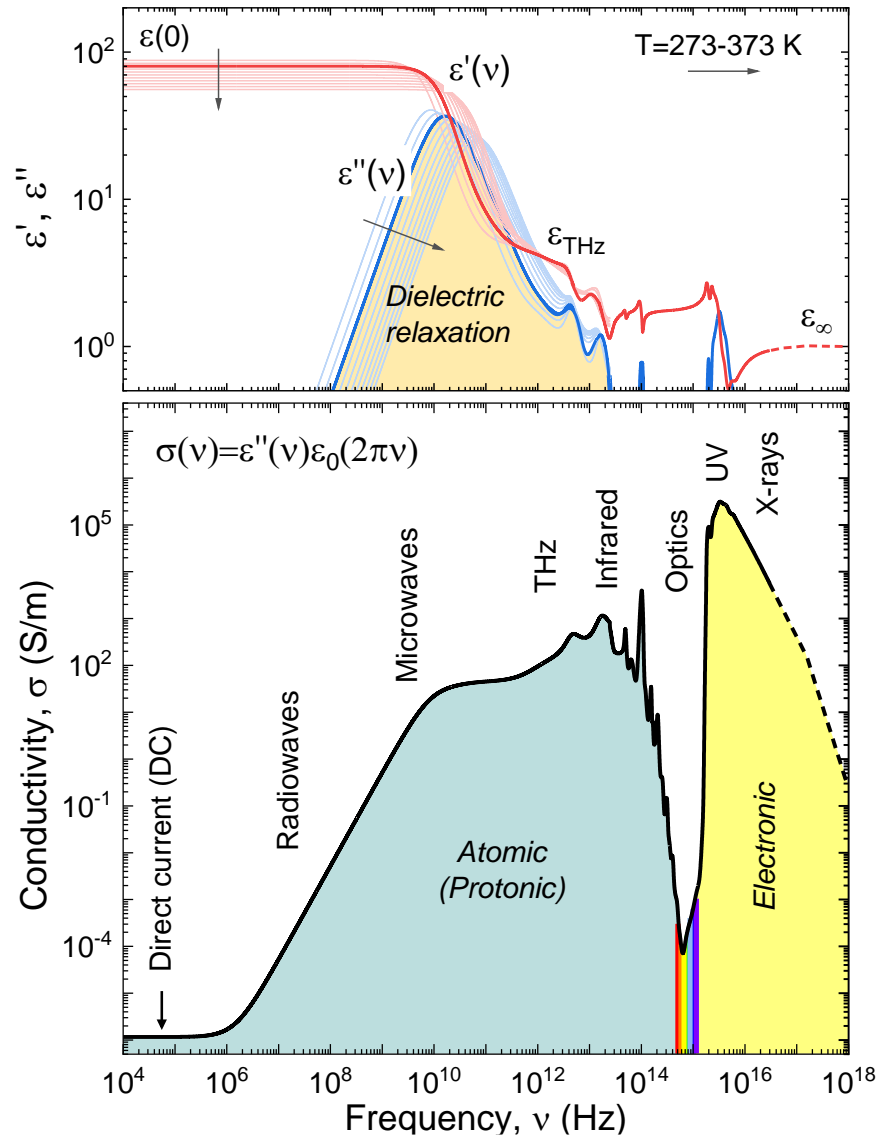


Dielectric constant: $\epsilon(0) = 1 + \frac{4\pi N\mu^2}{3Vk_B T}$ \Rightarrow $\epsilon(0)_{calc} \approx 14$ \longleftrightarrow $\epsilon(0)_{exp} \approx 80$



“We can't solve problems by using the same kind of thinking we used when we created them.”

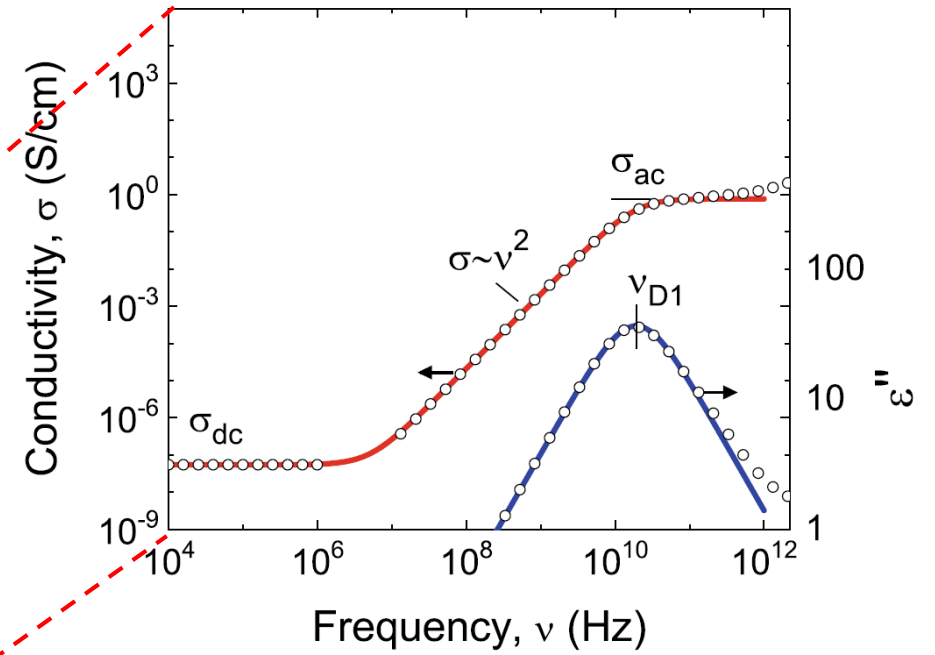
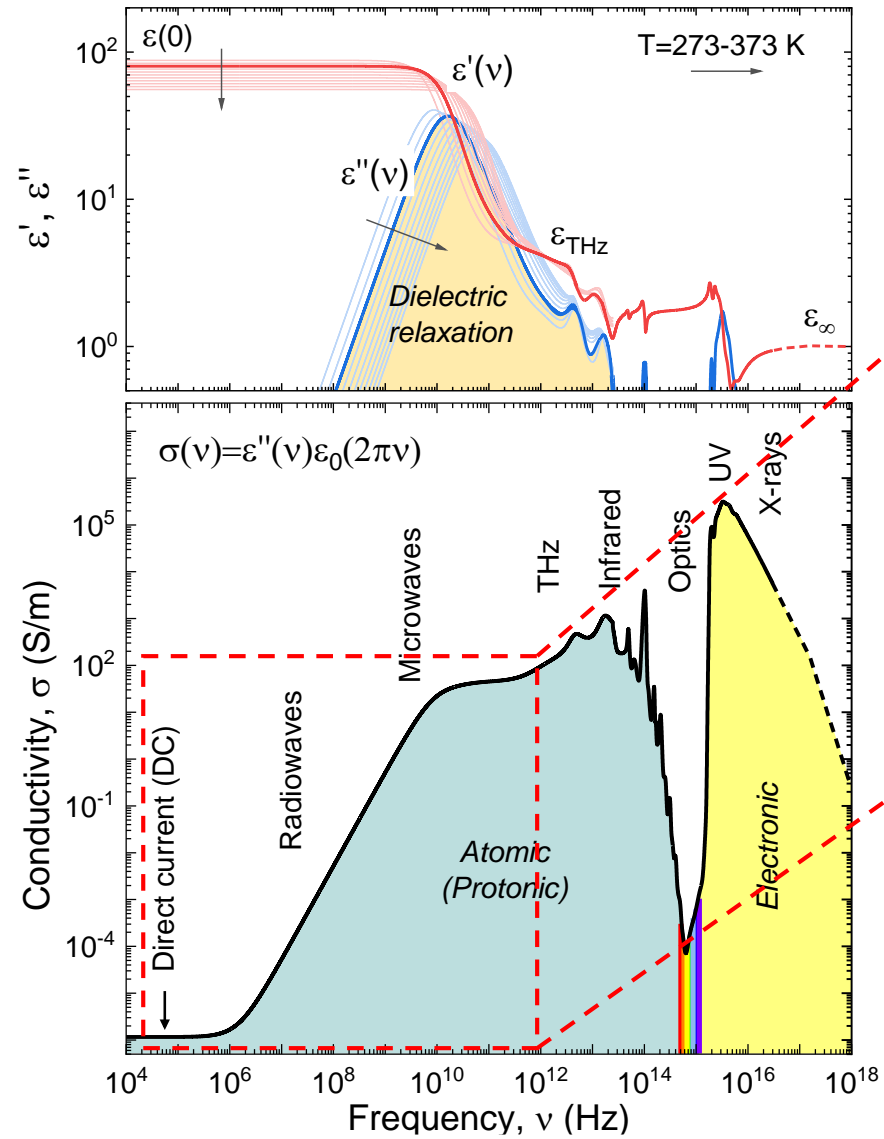
Dynamic conductivity of water: a different type of thinking



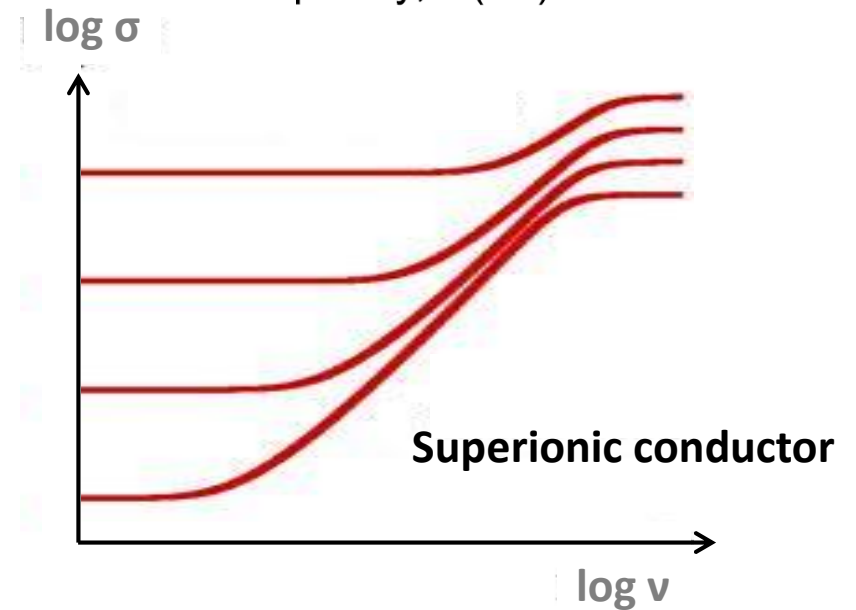
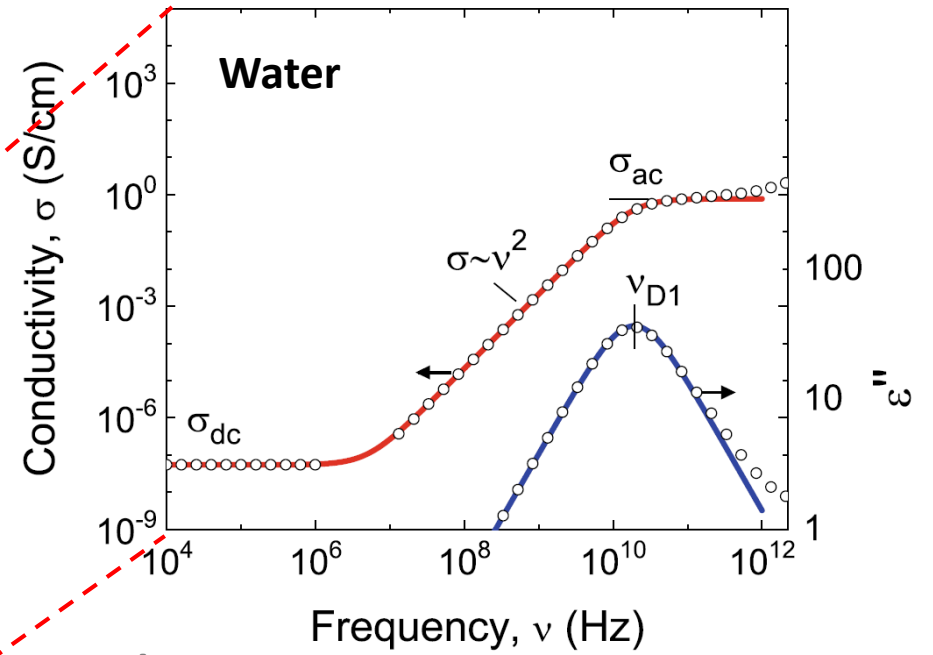
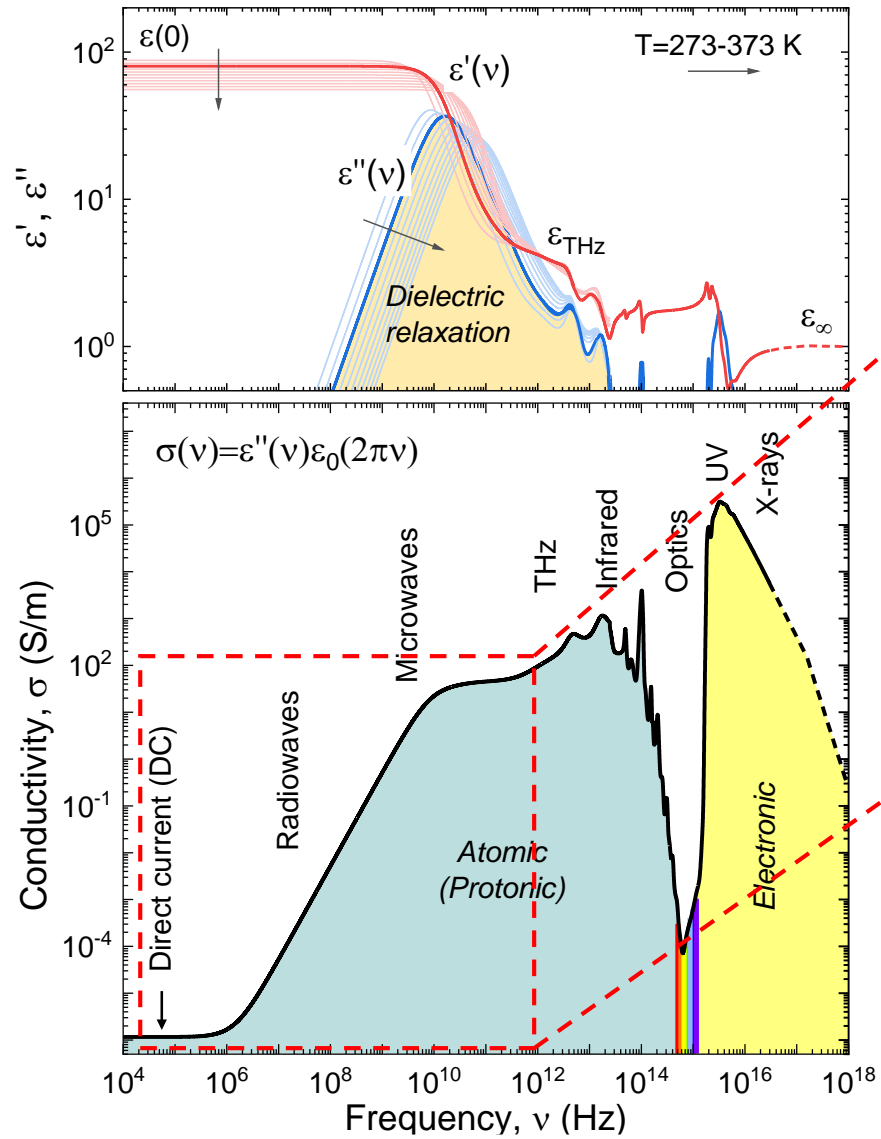
← Dielectric permittivity
(dielectric loses per period of the field)

← Dynamic conductivity
(dielectric loses per period of time)

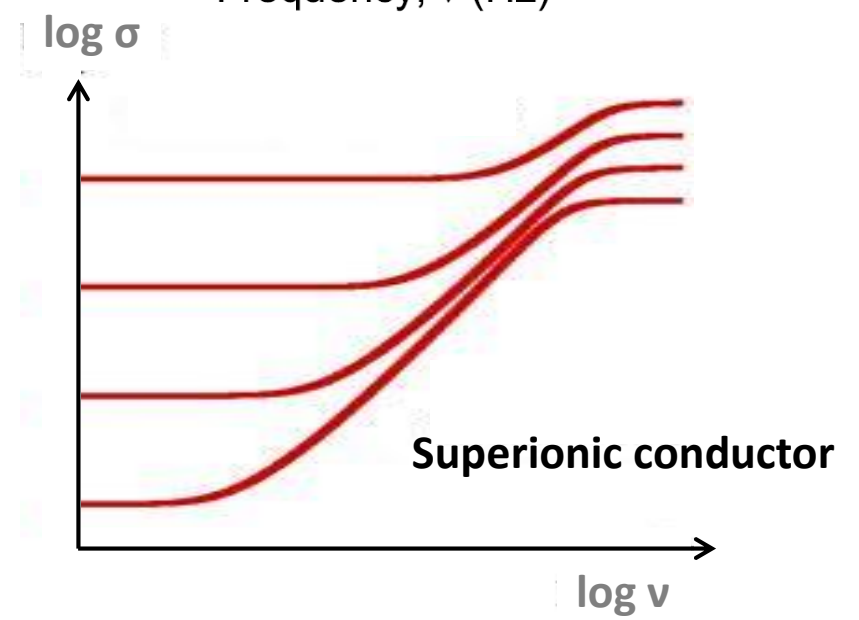
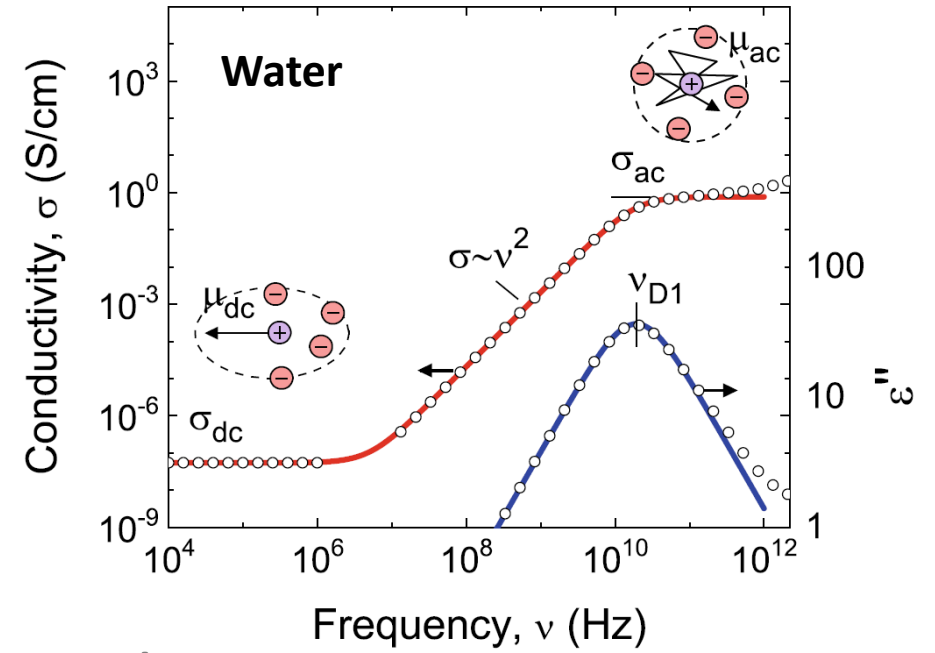
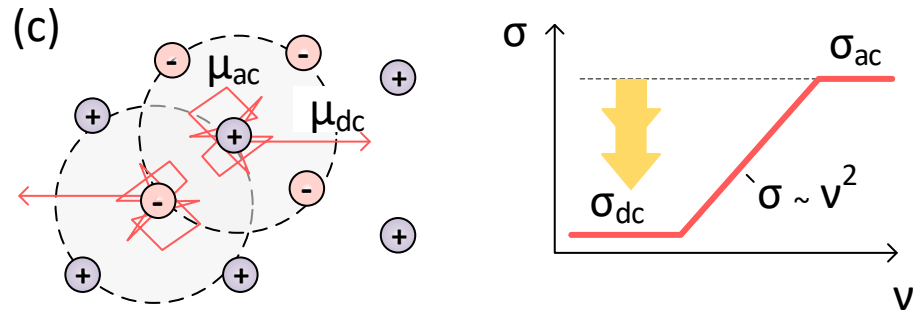
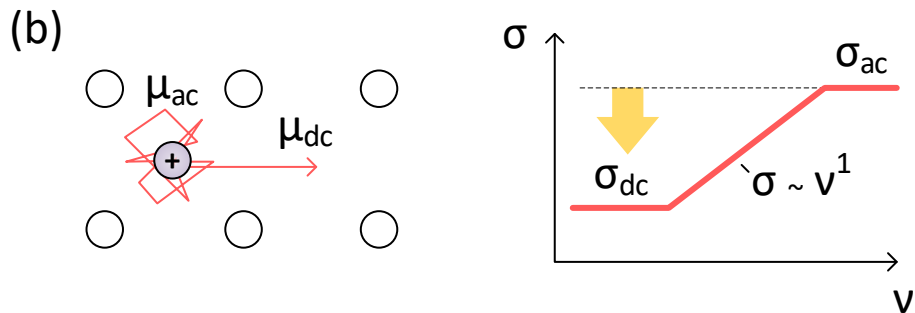
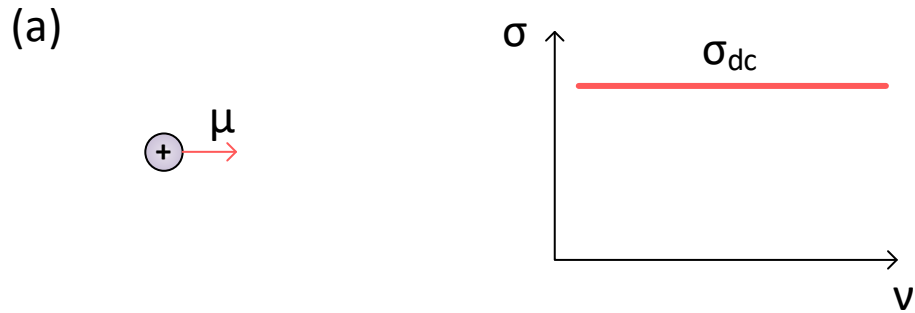
Dynamic conductivity of water



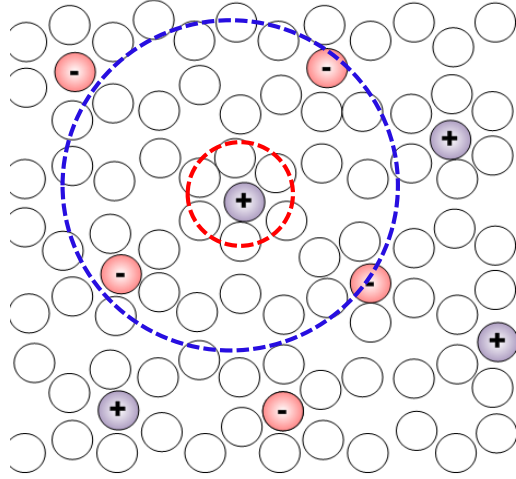
Dynamic conductivity of water



Dynamic conductivity and mobility

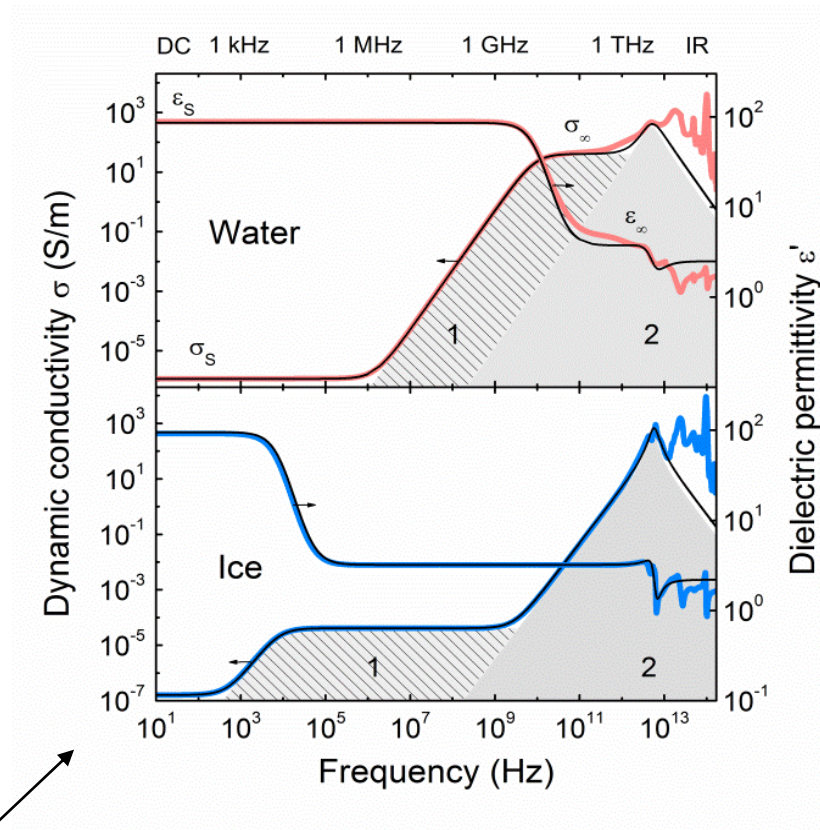


Turning on ion-ion interaction



$$\begin{cases} m\ddot{x} + m\gamma\dot{x} + \kappa_2 \int_0^t M(t-t')\dot{x}(t')dt' + K = f(t) \\ m^*\ddot{X} + m^*\Gamma\dot{X} - K = F(t), \end{cases}$$

$$\sigma(\omega) = \frac{in_i q^2 B}{(\kappa_1 / \omega)^2 - AB}$$

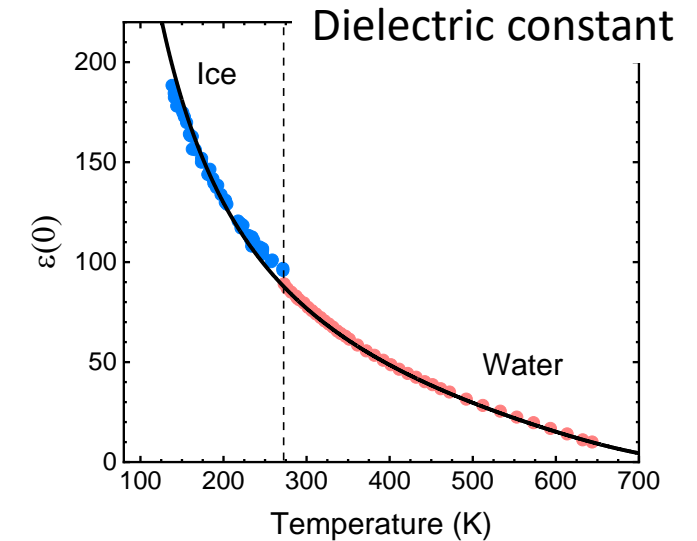
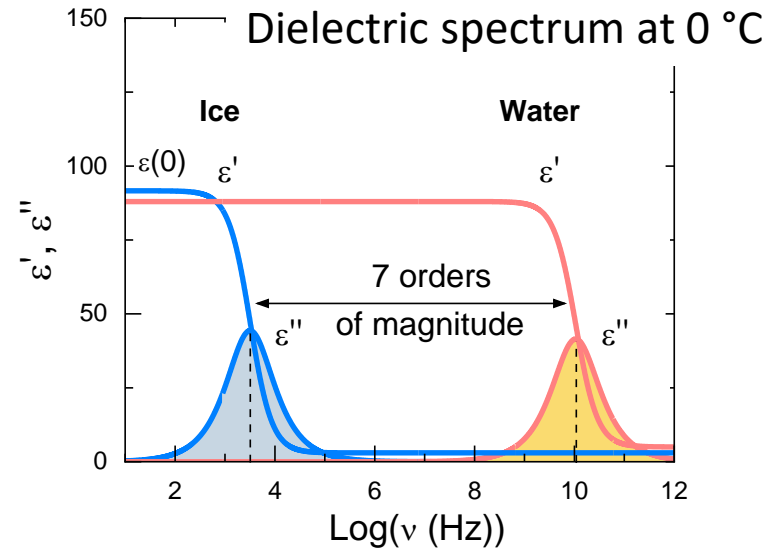
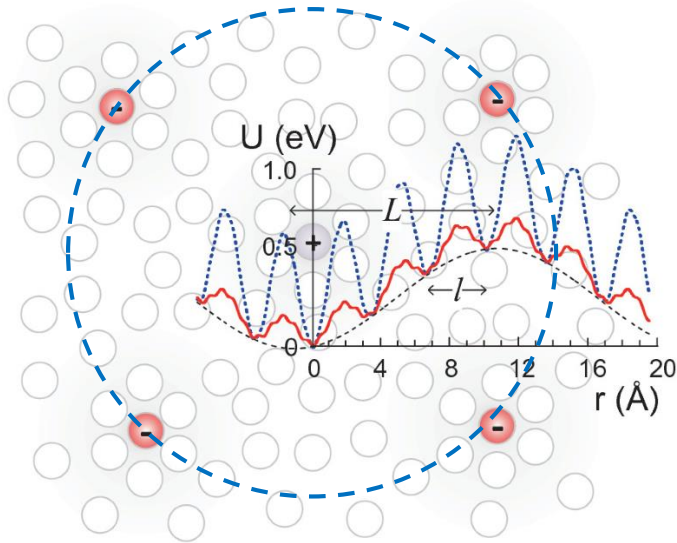


$$A = \kappa_1 / \omega - m[\omega + i(\gamma + \omega_0^2 M(\omega))] \text{ and } B = \kappa_1 / \omega - m^* \omega + im^* \Gamma, M(\omega) = 1 / (\tau_c^{-1} - i\omega)$$

Fit parameters for water: $n_f=1$ M (2%), $\gamma = 4$ THz, $\Gamma = 2.2$ THz, $\tau_c = 0.7$ ms, $\omega_0 = 0.7$ THz, $\Omega_0 = 5$ THz

Fit parameters for ice: $n_f=1$ M (2%), $\gamma = 3$ THz, $\Gamma = 2.4$ kHz, $\tau_c = 0.6$ ms, $\omega_0 = 0.6$ THz, $\Omega_0 = 5$ THz

Ice and water: similar structures, different dynamics



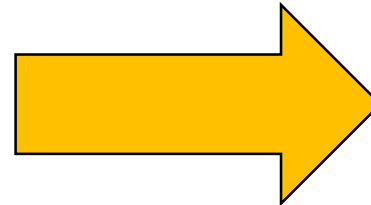
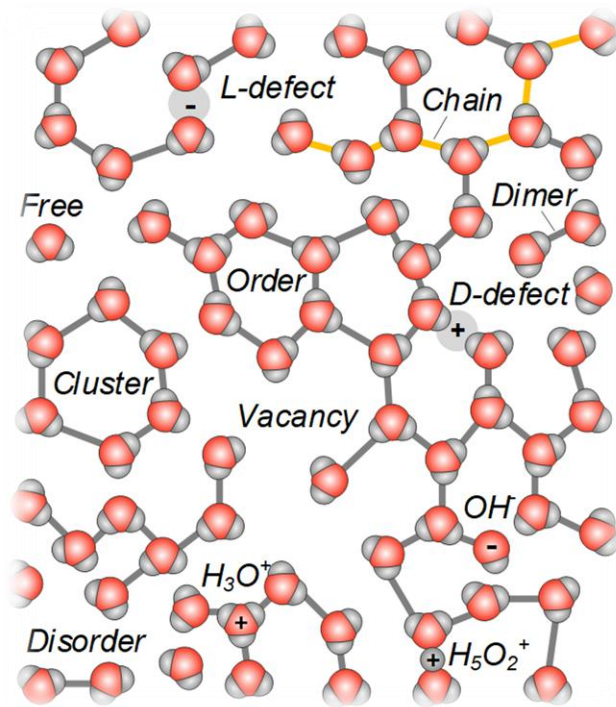
$$\epsilon_s = \frac{n_i q^2 (m^* \Gamma + \kappa_1 \tau_c)}{\epsilon_0 \kappa_1 (m \gamma + \kappa_2 \tau_c + m^* \Gamma)} \approx \frac{n_i q^2}{\epsilon_0 \kappa_2}$$

Fit parameters for water: $n_f=1$ M (**2%**), $\gamma=4$ THz, $\Gamma=2.2$ THz, $\tau_c=0.7$ ms, $\omega_0=0.7$ THz, $\Omega_0=5$ THz

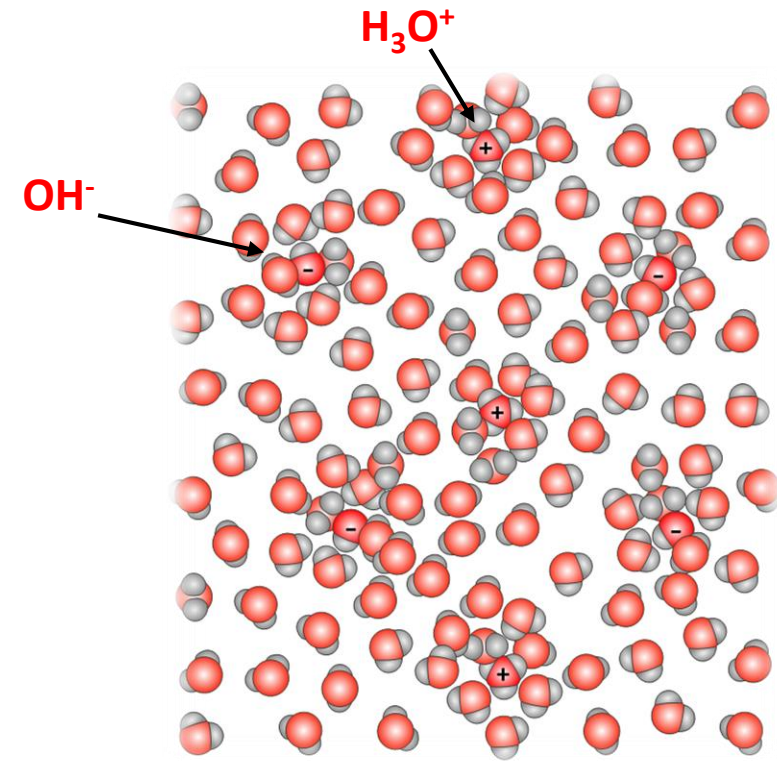
Fit parameters for ice: $n_f=1$ M (**2%**), $\gamma=3$ THz, $\Gamma=2.4$ kHz, $\tau_c=0.6$ ms, $\omega_0=0.6$ THz, $\Omega_0=5$ THz

A comparison of water structures

Bernal-Fowler model of water



The ionic model of water



2% of H₃O⁺ and OH⁻

pH and ion concentration

Concentration of ions according to the standard pH concept:

$$\text{pH}=7 \quad [\text{H}_3\text{O}^+] + [\text{OH}^-] \approx 10^{-9} \%$$

Compare with:

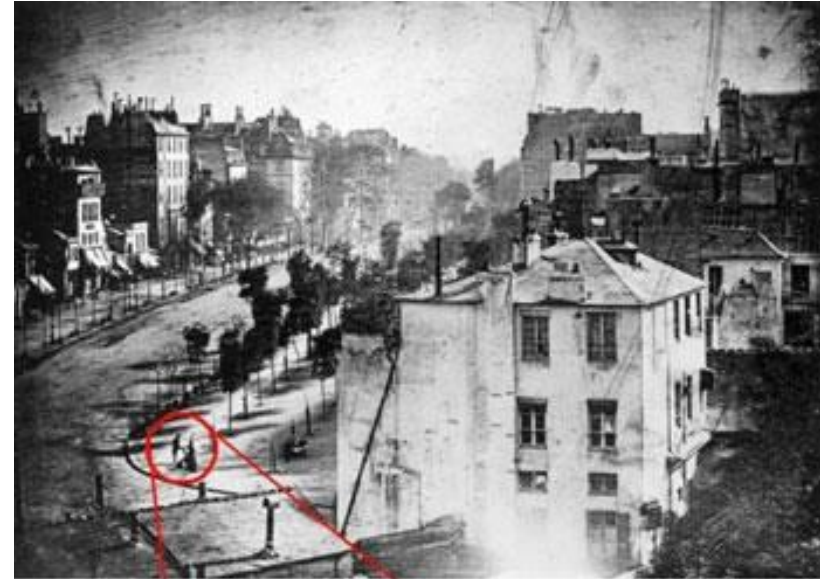
$$\text{HDO} \approx 10^{-2} \%$$

$$\text{H}_2\text{O}_2 \approx 10^{-7} \%$$

$$\text{CO}_2 \approx 10^{-4} \%$$

$$\text{O}_2 \approx 10^{-4} \%$$

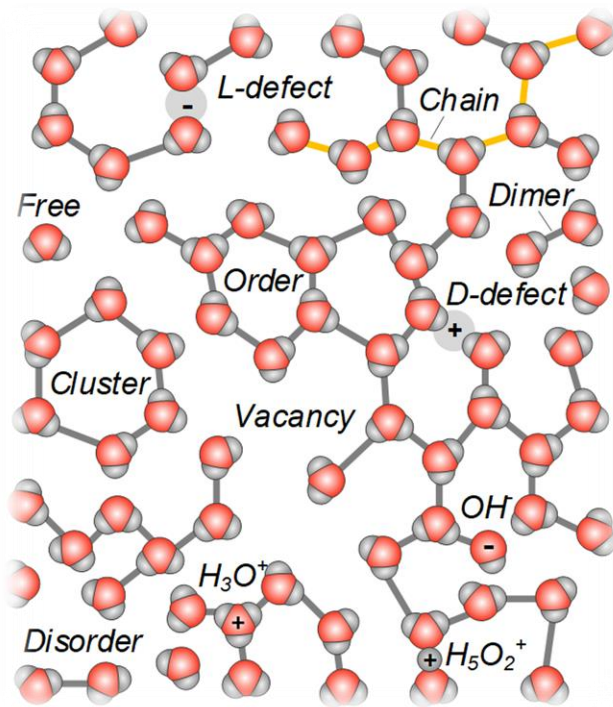
$$\text{N}_2 \approx 10^{-3} \%$$



Boulevard Du Temple, Louis Daguerre, 1838

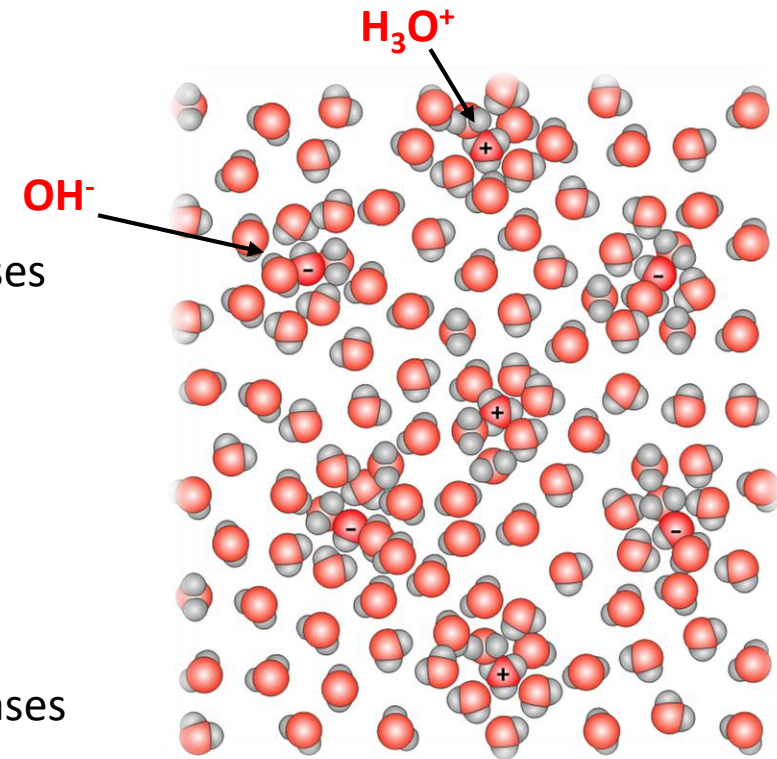
A comparison of water structures

Bernal-Fowler model of water
(Diffusion averaged picture)



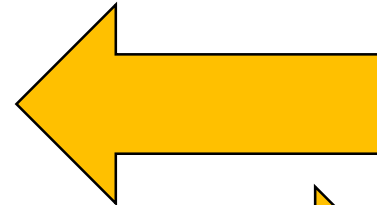
$$[\text{H}_3\text{O}^+] + [\text{OH}^-] \approx 10^{-9} \%$$

The ionic model of water
(Instantaneous structure)

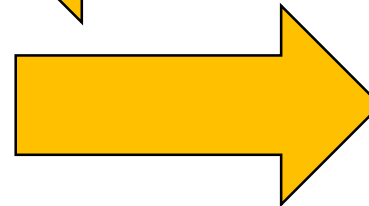


2% of H₃O⁺ and OH⁻

Observation time increases

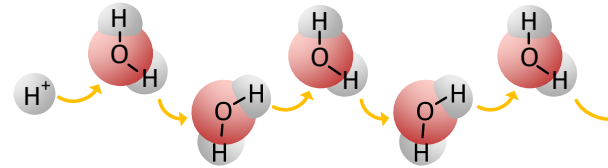


Observation time decreases

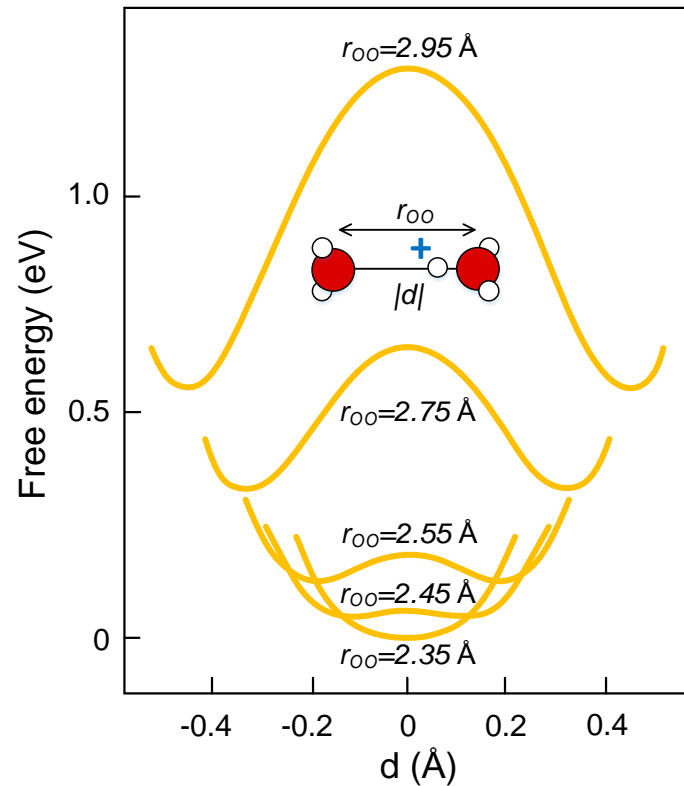


Quantum effects in water

Grotthuss mechanism:

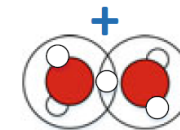


Proton tunneling:

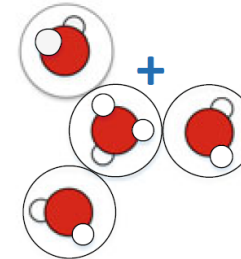


Two states of excess proton:

(a) $H_5O_2^+$ (Zundel)

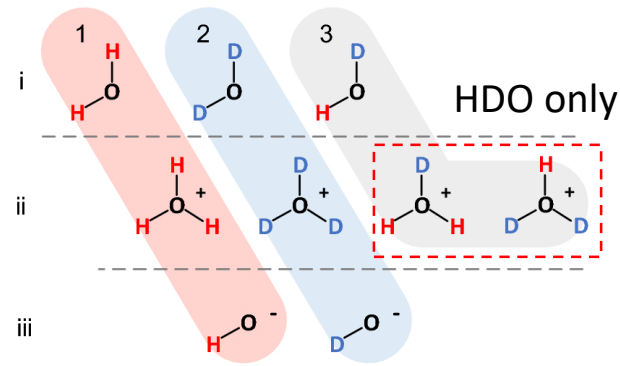
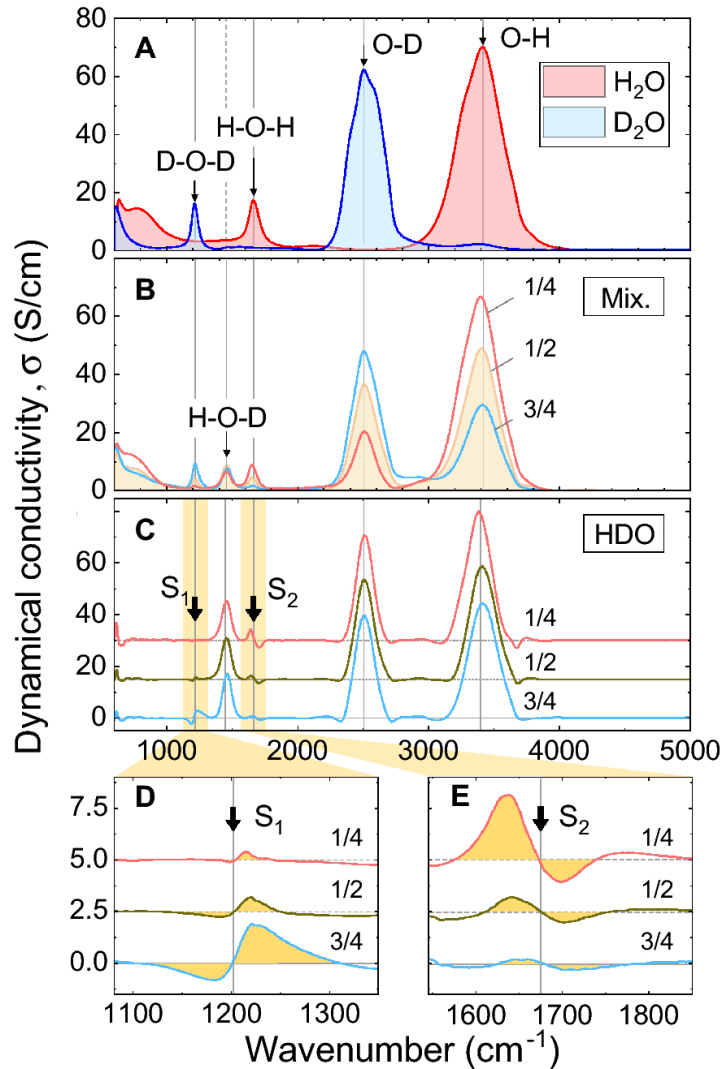


(b) $H_9O_4^+$ (Eigen)

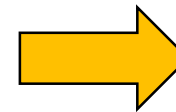
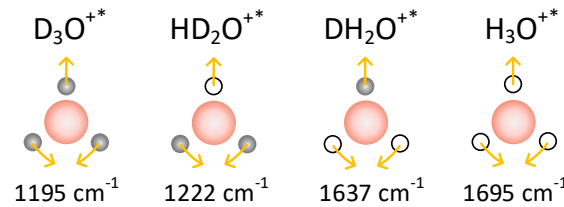
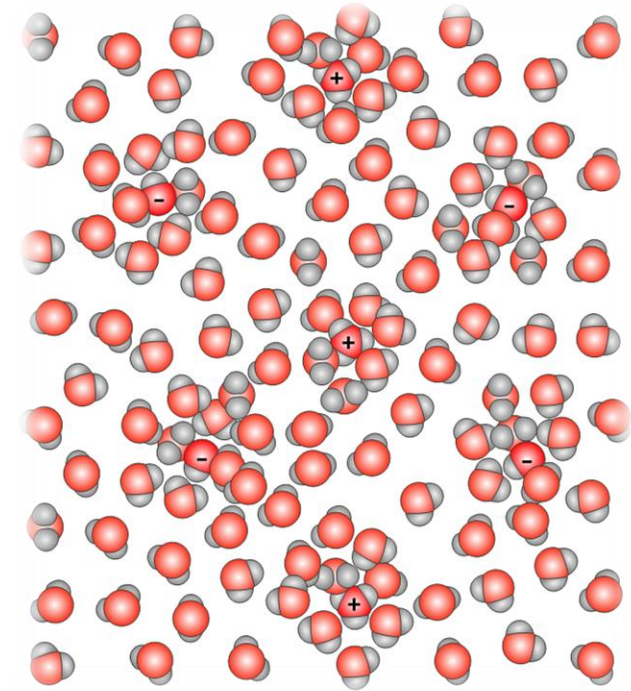


Where is the infrared signature of the excess protons?

Revealing excess protons in IR spectrum of water



The ionic model of water



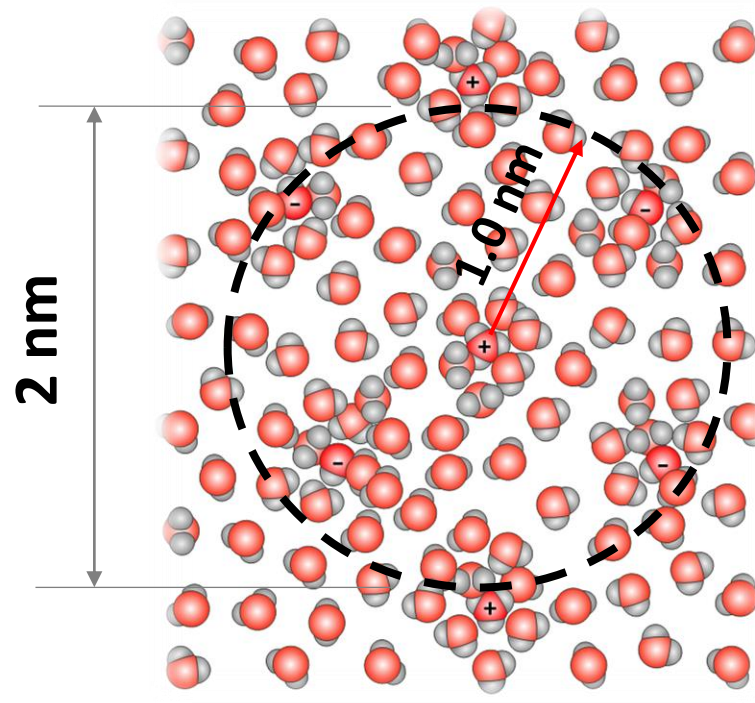
2% of H_3O^+ and OH^- **confirmed**

Lifetime of ion is 3 ps \rightarrow **time heterogeneity**

Space-time heterogeneity of water

The ionic model of water

2% of H_3O^+ and OH^-



V. G. Artemov, *PCCP*, 2019, 21, 8067

Lifetime of ions: 3 ps

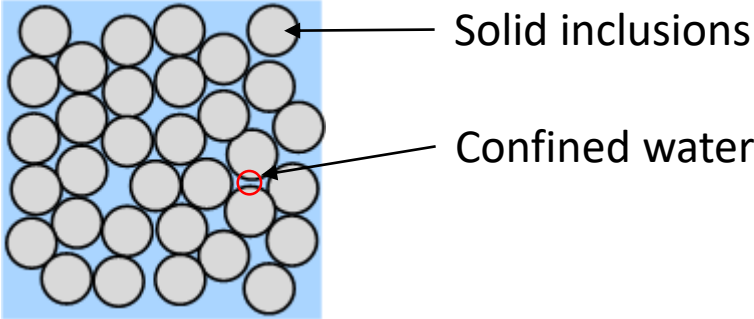
Lifetime of H_2O : 50 ps

Confined water: the test of spatial heterogeneity

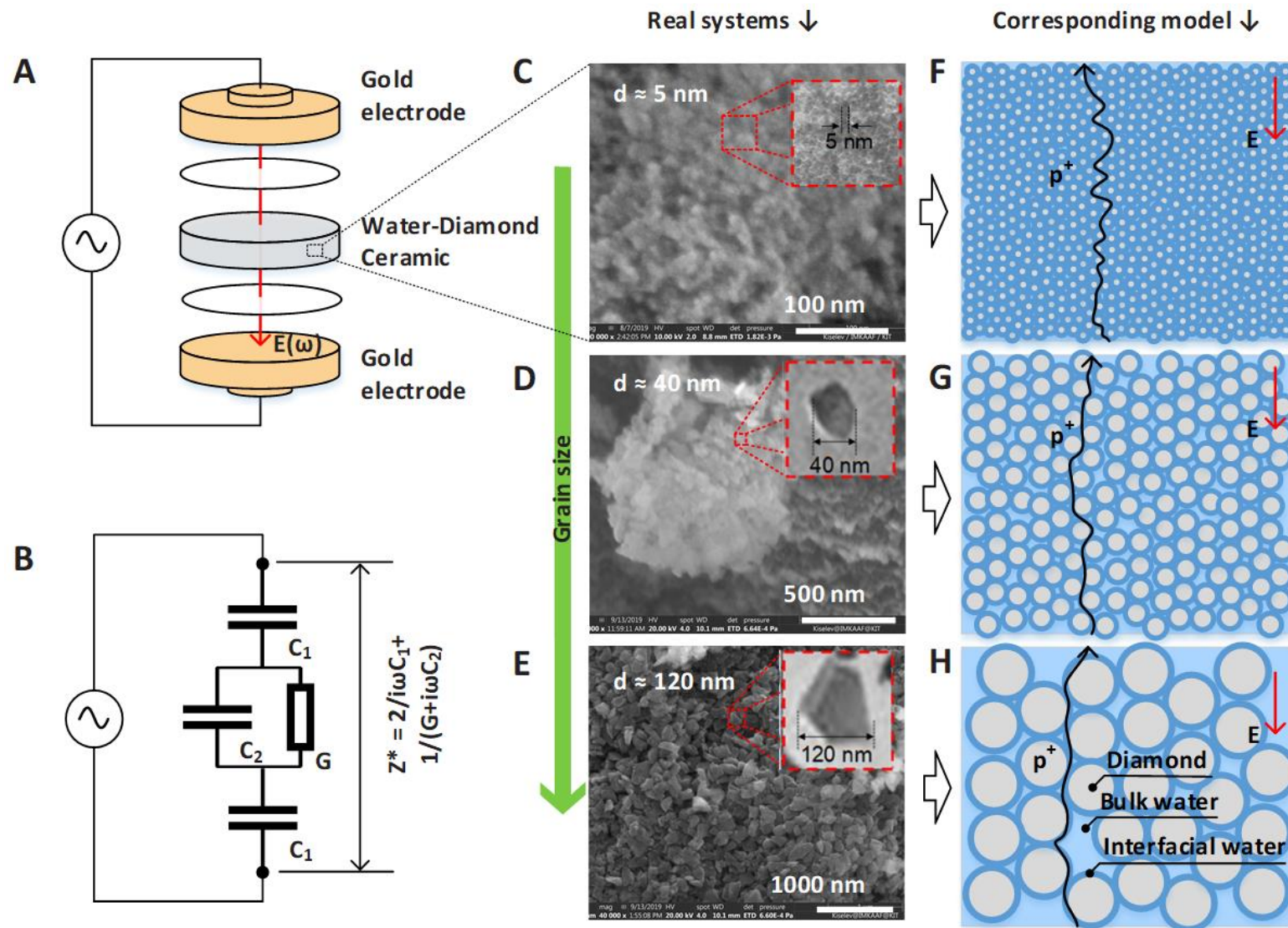
Bulk water



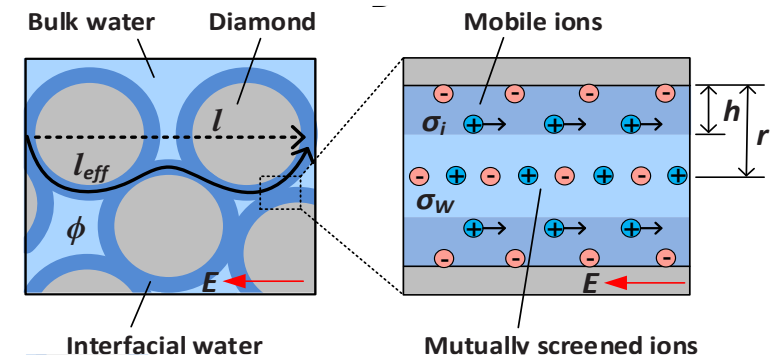
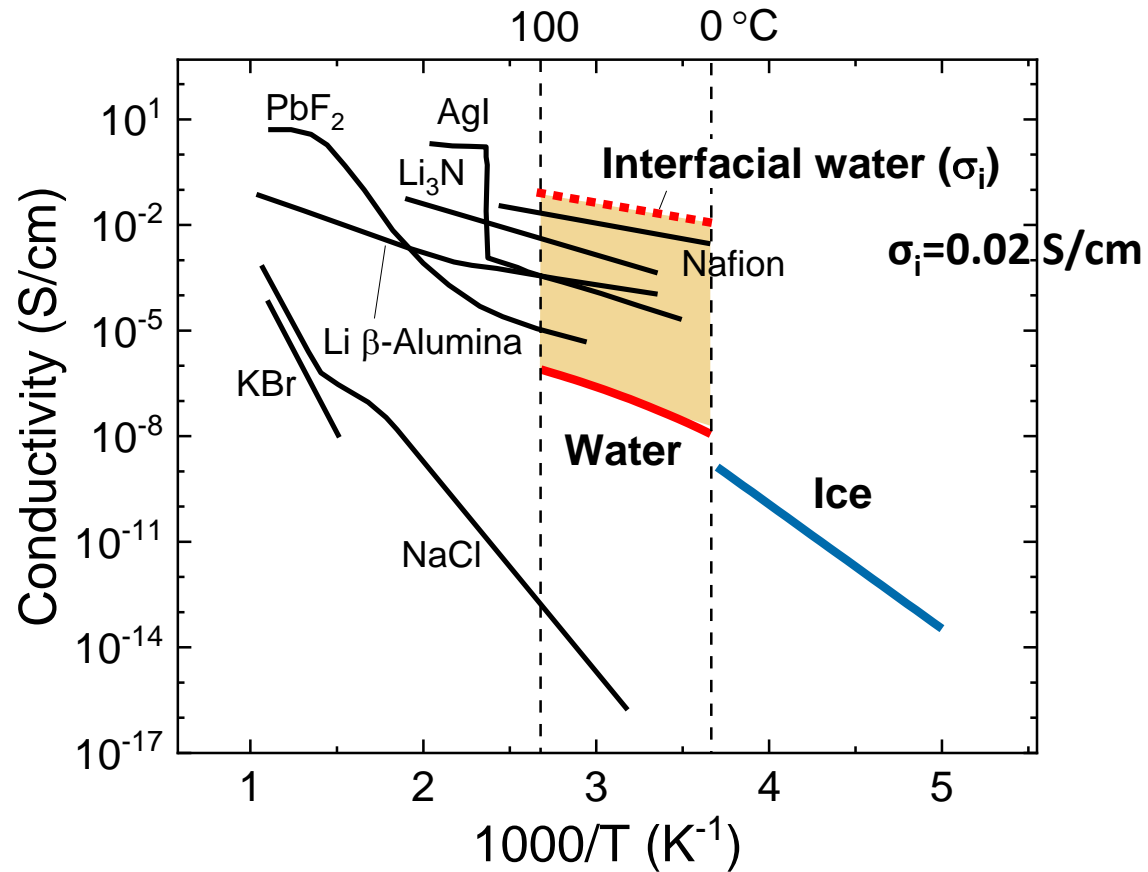
Water in porous matrix



Electric properties of water confined in nanopores



Water as superionic conductor



Conclusions (insights from broadband dielectric spectroscopy)

1. The century-old Bernal-Fowler model misses a part of the information because it is based on either static or optic data and excludes quantum effects.
2. We suggest the ionic model of water, which accounts for the quantum effects. According to the model, the concentration of H_3O^+ and OH^- ions is 2% and a lifetime of 3 ps. The model works for various electrodynamic properties in bulk and confinement.
3. The ionic model of water has a spatial heterogeneity period of 2 nm and a time heterogeneity period of 3 ps. We anticipate the changes in the properties of water near these points, such as change of viscosity, change of the dielectric constant, thermodynamic anomalies, etc.
4. We observed anomalously high proton conduction of the interfacial water. The effect paves the way for cheap and ecologically friendly devices for electrochemical energy storage.

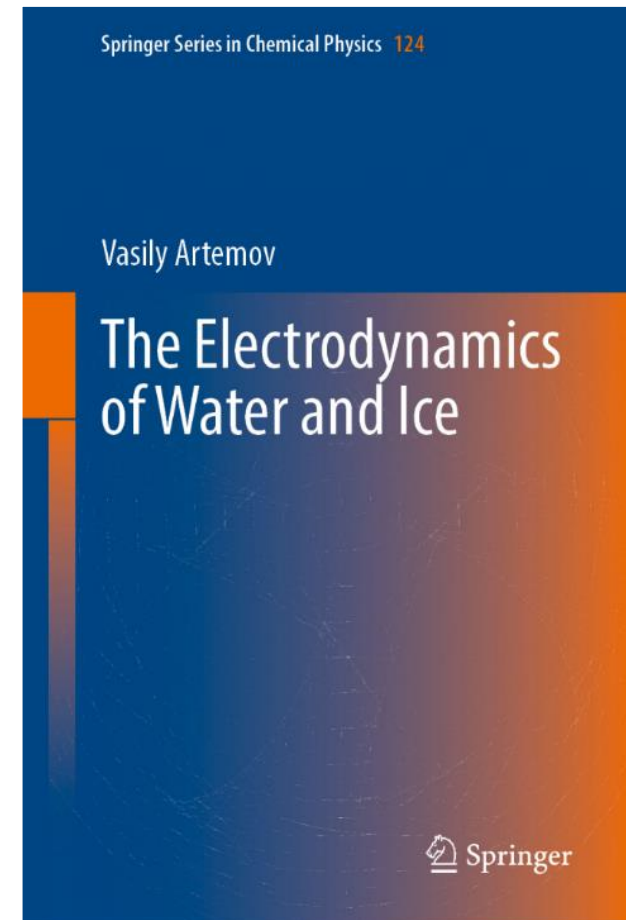
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Seulki Roh
Martin Dressel
Svetlana Ponomarenko



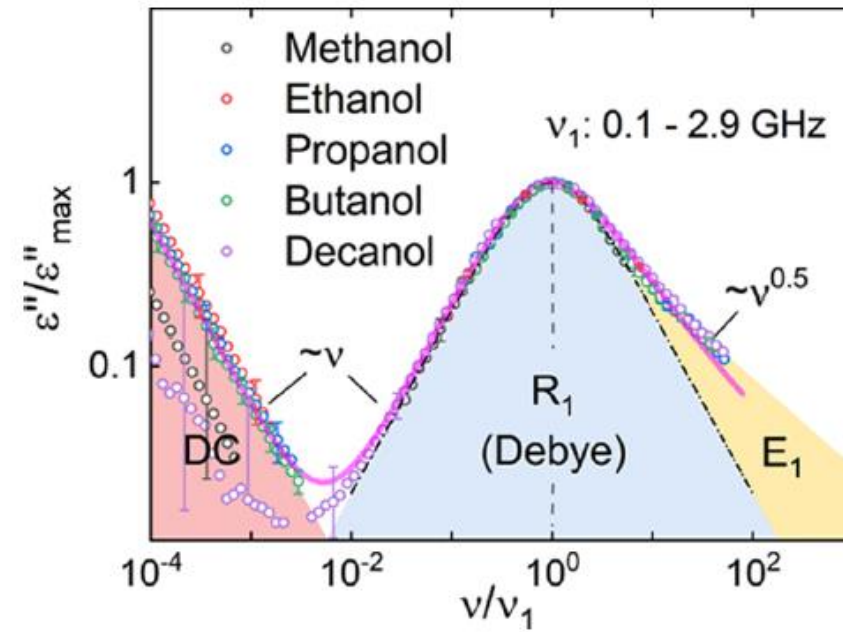
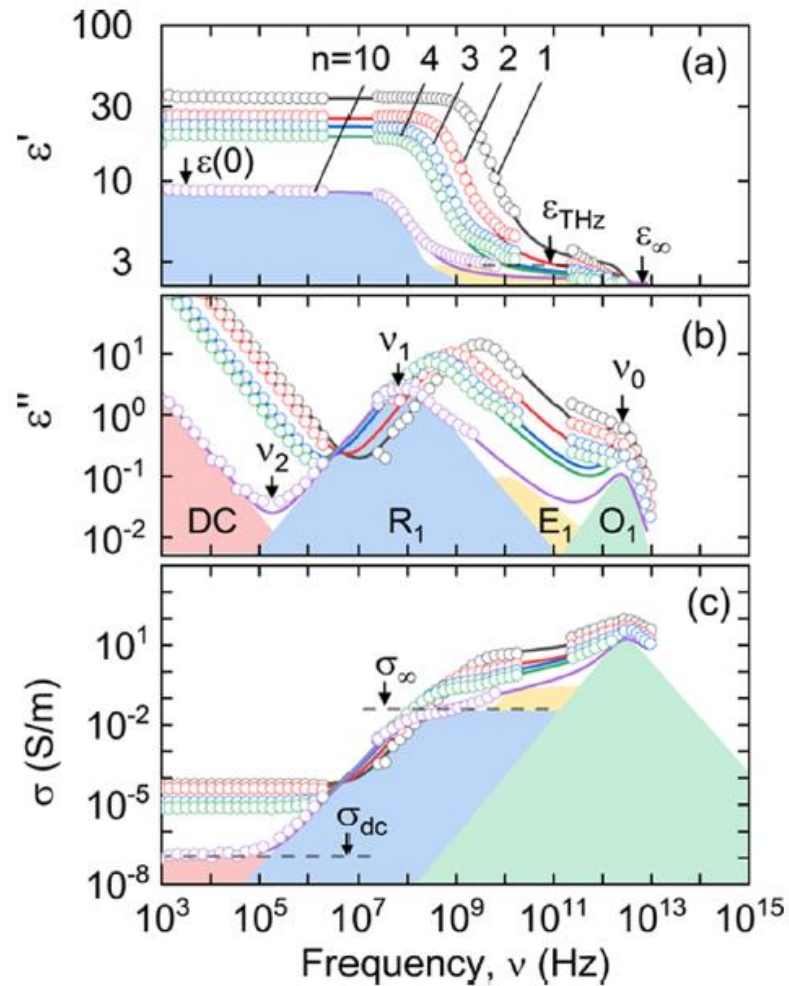
Thank you.

v.artemov@skoltech.ru



Vasily Artemov, 2021

Dielectric relaxation of monohydric alcohols



Artemov et al. *J. Phys. Chem. B* **2020**, 124, 11022–11029